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I. Solve the following integrals. SHOW THE STEPS OF YOUR PROCEDURE. (20 points each)

1. $\int \sin^3(2x) dx$

$= \int \sin(2x) \sin^2(2x) dx = \int \sin(2x) (1 - \cos^2(2x)) dx = \int \sin(2x) - \sin(2x) \cos^2(2x) dx$

$-\frac{\cos(2x)}{2} + \frac{\cos^3(2x)}{6} + C$

↓ they are the same

$\frac{\cos^3(2x)}{6} - \frac{\cos(2x)}{2} + C$

2. $\int x^6 \cos^2(x^7) dx$

$= \int x^6 (\frac{1}{2}(1 + \cos(2x^7))) dx = \frac{1}{2} \int x^6 + x^6 \cos(2x^7) dx = \frac{1}{2} [\frac{x^7}{7} + \frac{\sin(2x^7)}{14}] + C$

$\frac{x^7}{14} + \frac{\sin(2x^7)}{28} + C$

3. $\int 9x^4 \tan^3(x^5) dx$

$= \int 9x^4 (\tan(x^5) (\tan^2(x^5))) dx = \int 9x^4 ((\tan(x^5)) (\sec^2(x^5) - 1)) dx =$

$\int 9x^4 \tan(x^5) \sec^2(x^5) - 9x^4 \tan(x^5) dx = \frac{9 \tan^2(x^5)}{10} + \frac{9 \ln|\cos(x^5)|}{5} + C$

$$4. \int x^3 \sin^2(x^4) dx = \int v^3 \left(\frac{1}{2} (1 - \cos 2v) \right) dv = \frac{1}{2} \int v^3 - v^3 \cos 2v dv = \frac{1}{2} \left[\frac{v^4}{4} - \frac{\sin 2v^4}{8} \right] =$$

$$\frac{x^4}{8} - \frac{\sin 2x^4}{16} + C$$

$$5. \int \cot^2(5x) dx = \int (\csc^2(5x) - 1) dx = -\frac{\cot(5x)}{5} - x + C$$

BONUS (8 POINTS)

$$\int \cos^5(3x) dx$$

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