Task A-0: Angle at Centre and Angle at Circumference

Step 1

Create a circle.

Rename the centre as O and the point on the circumference as Z.

Hide point Z.

Step 2

Create points A, B and C on the circumference.



Refer to the figure, draw the line segments and create $\angle AOC$, $\angle ABC$ and their reflex angles.

Rename the angles as p, q, r and s as in the figure.

Set the colour of the angles at centre as red and the angles at circumference as blue.

Step 4

We want to show the pair p and r if r < s, otherwise show the pair q and s.

Right click on r, select object properties and choose the "Advanced" panel. In the field "Condition to Show Object", type "r<s", do the same for the angle p

Right click on s, select object properties and choose the "Advanced" panel. In the field "Condition to Show Object", type "s<r", do the same for the angle q



Step 5

Insert text |ABC| to show the sizes of $\angle ABC$ and ∠AOC.

The size of $\angle ABC$ is r if r < s, otherwise it is s. This can be written as if[r<s, r, s].

The size of $\angle AOC$ is the corresponding "partner" of r and s. If r < s, it is p, otherwise it is q, i.e. if [r < s, p, q].

Angle at centre = 118.74° Angle at circumference = 59.37°



Step 6

red

Insert text $|^{ABC}|$ to show the ratio between $\angle ABC$ and $\angle AOC$. To create a fraction, we use the \frac{numerator}{denominatior} LaTeX command



~ End of Task A-0 ~

Task A: Angle at Centre and Angle at Circumference

Step 1 Create a circle.

Rename the centre as O and the point on the circumference as Z. Hide point Z.

<u>Step 2</u> Create points A, B and C on the circumference.

Create their opposite points by using "Reflect Object about Point" •••.



<u>Step 3</u>

To create a point P that act as a "phantom" of A and snap to the point F, we use the command "DynamicCoordinates".

The format of the command is **DynamicCoordinates**[**<Point A>**, **<Number X>**, **<Number Y>**] When the new point moves, A moves with it and the coordinates of the new point are (X, Y) and usually X and Y depends on the coordinates of A.



At the **input** area, type

Q = DynamicCoordinates[C, If[Distance[C, B'] < 0.2, x(B'), x(C)], If[Distance[C, B'] < 0.2, y(B'), y(C)]]

<u>Step 6</u> Hide points A, A', B', C and C'. Rename P as A and Q as C. Change the color of A, B, and C to black.

Step 7

Refer to the figure, draw the line segments and create $\angle AOC$, $\angle ABC$ and their reflex angles.

Rename the angles as p, q, r and s as in the figure. Set the colour of the angles at centre as red and the angles at circumference as blue.



<u>Step 8</u>

We want to show the pair p and r if r < s, otherwise show the pair q and s.

Right click on r, select object properties and choose the "Advanced" panel. In the field "Condition to Show Object", type "r<s", do the same for the angle p

Right click on s, select object properties and choose the "Advanced" panel. In the field "Condition to Show Object", type "s<r", do the same for the angle q

<u>Step 9</u>

Insert text ABC to show the sizes of $\angle ABC$ and $\angle AOC$.

The size of $\angle ABC$ is r if r < s, otherwise it is s. This can be written as if[r<s, r, s].

The size of $\angle AOC$ is the corresponding "partner" of r and s. If r < s, it is p, otherwise it is q, i.e. if[r<s, p, q].

<u>Step 10</u>

Insert text |ABC| to show the ratio between $\angle ABC$ and $\angle AOC$. To create a fraction, we use the LaTeX command \mathbf{rac} (numerator) (denomination)

 $\frac{\langle AOC \rangle}{\langle ABC \rangle} = \frac{if[r < s, p, q]}{\{if[r < s, r, s]}} = \frac{if[r < s, p, q]}{if[r < s, r, s]}$

<u>Step 11</u>

To change the colour of the numerator and denominator, we enclose the numerator by $\red{}$ and the denominator by $\blue{}$.

 $frac{red{if[r < s, p, q]}}{\delta [r < s, r, s]}}$



~ End of Task A ~

Task A-1:Angle at Centre and Angle NOT at CircumferenceStep 1Repeat Step 1 of Task A.

Step 2

Create a free point D on the plane. Then, create a line passing through the centre O and D. Mark one of the points of intersection of the line and the circle as E.

Hide the points D, E and the line.

<u>Step 3</u>

Create a point B with the dynamic coordinates depending on point D, while snapping to point E. (Exercise)

Step 4

Follow the rest of steps in Task A to complete the dynamic worksheet to show one constraint of the theorem by the counter-examples.

Task A-2:Angle at Centre and Angle at Circumference of an ELLIPSEStep 1

Create an ellipse. Label the mid-point of the foci as O.

Repeat all the other steps in Task A.

~ End of Task A-2 ~

Task A-3: Angle at Centre and Angle at "Circumference" of a SQUARE

Step 1

Create a square by using the "Regular Polygon" tool. Label the centre of the square as O.

Step 2

Create Sq as a list of item holding the four segments of the square using the bracket "{}". Define points A, B, C as "point[Sq]".

Repeat all the other steps in Task A.

~ End of Task A-3 ~

Think about it:

Student QQ claims that if $\beta = 2\alpha$, D must be the centre of the circle. Do you agree? Explain your answer.

