## Div 2 - Elective GeoGebra, Art \& Math

## FIBONACCI SPIRAL - part 1

## Period 1 (paper and pencil)

Use graph paper to make a Fibonacci spiral using pencil and compass.
Materials:

- print grid 1 cm (3 copies each student)
- compass
- markers / pencils


## Period 2 (GeoGebra)

Step one: create a new ggb tool
Step two: crate a Fibonacci spiral
adapted from:
https://www3.risc.jku.at/conferences/cadgme2009/Judith Hohenwarter/presentation files/Ge oGebra WS 7.pdf)

Homework creative paper work

## FIBONACCI SPIRAL - part2

- How to Review Steps of Construction
- Create a check box
- Use the slider
- Create a Fibonacci animated (beating) heart


## Creating a Square Tool

## Preparations

- Open a new GeoGebra classic
- Hide the algebra window, input field, and coordinate axes
- Change the labeling setting to All new objects


## Step by step

| 1 | Segment a with endpoints $A B$ |
| :---: | :---: |
| 2 j | Perpendicular line $b$ to segment $A B$ through point $B$ |
| $3 \ominus$ | Circle c with center $B$ through point $A$ |
| $4>$ | Intersect circle $c$ and perpendicular line $b$ to get intersection point $C$ |
| $5 \geqslant$ | Parallel line $d$ to perpendicular line $b$ through point $A$ |
| $6 \rightarrow$ | Parallel line $e$ to segment $a$ through point $C$ |
| $7>$ | Intersect lines $d$ and $e$ to get intersection point $D$ |
| 8 D | Square $A B C D$ |
| 9 ○ | Hide auxiliary objects (lines and circle). |
| 10 A A | Hide labels of all objects. |
| 11 | Set the square's color to black and set the filling to 0\%. |
| 12 呺 | Create your square tool (menu Tools - Create new tool...). <br> Output objects: square, sides of the square, points $C$ and $D$ <br> Input objects: points $A$ and $B$ <br> Name: Square <br> Toolbar help: Click on two points |
| 13 | Save your square tool as file Square_Tool.ggt <br> Hint: Menu Tools - Manage tools... - Save as... |

## Creating a Fibonacci Spiral

A Fibonacci spiral can be created by drawing arcs connecting the opposite corners of squares in the Fibonacci tiling which uses squares of sizes $1,1,2,3,5,8$, 13, 21,...


## Preparations

- Show the grid


## Instructions

1 Use your Square tool to create a square with side length 1
Hint: Place the two points on grid points that are next to each other.
2 Create a second square with side length 1 below the first square.
Hint: Use already existing points to connect both squares.
3 Create a third square with side length 2 on the right hand side of the
4 Continue creating squares with side lengths $3,5,8$, and 13 in counter clockwise direction.
5 -. Create a circular arc within the first square you created.
Hint: Specify the lower right vertex of the square as the center of the arc. Select two opposite vertices of the square in counter clockwise orientation.
6 Repeat step 5 for each of the squares in order to construct the Fibonacci spiral.

7 Enhance your construction using the Properties dialog.

## Homework:

Colored paper with a spiral printed to take home for a colage. Send email to parents.

## Some ideas to inspire



## FIBONACCI SPIRAL - part2

Show:

- How to Review Steps of Construction
- Create a check box
- Use the slider

| 3 File | $\stackrel{ }{*}$ |
| :---: | :---: |
| 1 - Edit |  |
| 0 Perspectives |  |
| A View |  |
| N. $\square$ Algebra <br> $\\| \mathrm{x}=\square \mathrm{CAS}$ <br> Graphics Graphics 2 3D Graphics Spreadsheet Probability Calculator |  |
| - Construction Protocol Input Bar Navigation Bar Sensors |  |
| Refresh Views <br> Recompute All Objects |  |
| Settings | - |

## Creating a Fibonacci Beating Heart



Step by step:

| 1 | Open your ggb file in which you created a square tool |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 2 | Save it with a different name. Example: Marina Fibonacci heart |  |  |  |  |  |
| 3 | Delete the entire construction |  |  |  |  |  |
| 4 | Create a slider |  |  |  |  |  |
|  | Slider |  |  | Slider |  |  |
|  | Name |  |  | Name |  |  |
|  | $a=1$ |  |  | $\mathrm{a}=1$ |  |  |
|  | - Number | $\bigcirc$ Angle | $\bigcirc$ Integer | - Number | $\bigcirc$ Angle | - Integer |
|  | Interval | Slider | Animation | Interval | Slider | Animation |
|  | Min: | Max: | Increment: | Speed: |  |  |
|  | 0.5 |  | 0.5 | 5 |  |  |
|  |  |  |  | Repeat: |  |  |
|  |  |  |  | $\Leftrightarrow$ Oscillating |  | - |
|  |  |  | OK Cancel |  |  | OK Cancel |
| 5 | Create a segment with a given length |  |  |  |  |  |
| 6 | Select the two points as your input for your square tool |  |  |  |  |  |
| 7 | Keep working on your spiral as you did before |  |  |  |  |  |
| 8 | Once your spiral is finished, you can color it, rotate and reflect to complete the heart |  |  |  |  |  |

