

TALLER DE LÍMITES

PROPIEDADES DE LOS LÍMITES.

$$\lim_{x \rightarrow a} x = a$$

$$\lim_{x \rightarrow a} k = k$$

$$\lim_{x \rightarrow a} (k * f(x)) = k * \lim_{x \rightarrow a} f(x) \quad \text{con } k \neq 0$$

$$\lim_{x \rightarrow a} (f \pm g)(x) = \lim_{x \rightarrow a} f(x) \pm \lim_{x \rightarrow a} g(x)$$

$$\lim_{x \rightarrow a} (f * g)(x) = \lim_{x \rightarrow a} f(x) * \lim_{x \rightarrow a} g(x)$$

$$\lim_{x \rightarrow a} \left(\frac{f}{g} \right)(x) = \frac{\lim_{x \rightarrow a} f(x)}{\lim_{x \rightarrow a} g(x)}$$

$$\lim_{x \rightarrow a} (f(x))^k = \left(\lim_{x \rightarrow a} f(x) \right)^k$$

$$\lim_{x \rightarrow a} (f(x))^{g(x)} = \left(\lim_{x \rightarrow a} f(x) \right)^{\lim_{x \rightarrow a} g(x)}$$

I. Resolver los siguientes límites algebraicos.

$$1. \lim_{x \rightarrow 1} 4$$

$$2. \lim_{x \rightarrow -1} 2x$$

$$3. \lim_{x \rightarrow -3} -3x$$

$$4. \lim_{x \rightarrow 0} 4 \cdot x^2$$

$$5. \lim_{x \rightarrow 3} -6 \cdot x^6$$

$$6. \lim_{x \rightarrow 3} -\frac{5}{8} \cdot x^4$$

$$7. \lim_{x \rightarrow -2} 6\sqrt{2} \cdot x^5$$

$$8. \lim_{x \rightarrow 1} 4x^3$$

$$9. \lim_{x \rightarrow -1} (4x^3 + x^2 + 2x + 1)$$

$$10. \lim_{x \rightarrow 5} (2x^3 - 3x^2 - x - 4)$$

$$11. \lim_{x \rightarrow -3} (x^3 + x^2 + 2x + 6)$$

$$12. \lim_{x \rightarrow 2} (5x^3 - x^2 - 3)$$

$$13. \lim_{x \rightarrow -1} (2x^3 + x + 7)$$

$$20. \lim_{x \rightarrow 0} (x^4 + 3x^3 - 4x^2 + x - 6)$$

$$21. \lim_{x \rightarrow 1} (3x^4 - 2x^2 + 10)$$

$$22. \lim_{x \rightarrow 4} (5x^4 - 2x + 6)$$

$$23. \lim_{x \rightarrow -3} (x^4 + 2x^3 + 5x^2 - 3x + 4)$$

$$24. \lim_{x \rightarrow 2} (3x^4 - 4x^3 + 5)$$

$$25. \lim_{x \rightarrow 2} (x^3 - x + 1) \cdot (2x^3 - 5)$$

$$26. \lim_{x \rightarrow 1} (2x^3 - 1) \cdot (2x^3 + 1)$$

$$27. \lim_{x \rightarrow -3} (4x^3 - 2x) \cdot (x^3 + x^2 + 1)$$

$$28. \lim_{x \rightarrow 3} (x^3 - 4)(2x^2 - 1)$$

$$29. \lim_{x \rightarrow 1} (3x^4 + 2x^2 - 1)(x^3 - 2)$$

$$30. \lim_{x \rightarrow -5} (x^4 - 3x)(x^3 + 4x^2 - 1)$$

$$31. \lim_{x \rightarrow -2} (3x^4 + x^2)(x^2 + 1)$$

$$32. \lim_{x \rightarrow 4} (x^2 + 2x + 3)(x + 1)$$

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|--|--|
| 14. $\lim_{x \rightarrow 4} (4x^3 - 2x^2)$ | 33. $\lim_{x \rightarrow -2} (2x^2 + 1)(3x - 4)$ |
| 15. $\lim_{x \rightarrow 2} (4x^3 - 5x^2 + 1)$ | 34. $\lim_{x \rightarrow 2} (4x^2 - 2)(5x + 1)$ |
| 16. $\lim_{x \rightarrow -1} (3x^5 - 8x + 3)$ | 35. $\lim_{x \rightarrow 1} (3x - 4)(x^2 + 5x)$ |
| 17. $\lim_{x \rightarrow 4} (3x^4 + 2x^3 - x^2 + x - 6)$ | 36. $\lim_{x \rightarrow 0} (2x^2 + 4x - 1)(2x - 4)$ |
| 18. $\lim_{x \rightarrow 3} (2x^4 + 3x^2 - 5)$ | 37. $\lim_{x \rightarrow -2} (3x^2 + 4x - 1)(x^2 + 1)$ |
| 19. $\lim_{x \rightarrow -2} (4x^4 + 3x^3 - x + 1)$ | 38. $\lim_{x \rightarrow 3} (x^2 + x - 1)(2x^2 - x)$ |

II. Calcula los siguientes límites

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|---|---|
| 1. $\lim_{x \rightarrow 2} \left(\frac{x^3 + 2x + 3}{x^2 + 5} \right)$ | 6. $\lim_{x \rightarrow 1} \left(\frac{4x - 1}{2x^2 - 3x + 4} \right)$ |
| 2. $\lim_{x \rightarrow -1} \left(\frac{2x + 1}{x^2 - 3x + 4} \right)$ | 7. $\lim_{x \rightarrow 3} \left(\frac{3x^2 - 1}{4x^2 + 2} \right)$ |
| 3. $\lim_{x \rightarrow -3} \left(\frac{x^2 - 9}{2x^2 + 7x - 3} \right)$ | 8. $\lim_{x \rightarrow -5} \left(\frac{x^3 - 5}{3x^3 + x^2 - 5} \right)$ |
| 4. $\lim_{x \rightarrow 4} \left(\frac{x^2 - 4x + 1}{3x^2 - 2x + 1} \right)$ | 9. $\lim_{x \rightarrow 0} \left(\frac{x^3 - 4x^2 + x - 1}{2x^2 + 4x - 1} \right)$ |
| 5. $\lim_{x \rightarrow 0} \left(\frac{x^2 - 3x}{x + 1} \right)$ | |

III. Encuentra el valor del límite.

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|---|---|
| 1. $\lim_{x \rightarrow 5} \left(\frac{x^2 - 25}{x - 5} \right)$ | 6. $\lim_{x \rightarrow 1} \left(\frac{2x^2 - 3x + 1}{x + 1} \right)$ |
| 2. $\lim_{x \rightarrow 0} \left(\frac{x^2 + x}{3x^2 + 2x} \right)$ | 7. $\lim_{x \rightarrow -2} \left(\frac{x^3 - x^2 - x + 10}{x^2 + 3x - 2} \right)$ |
| 3. $\lim_{x \rightarrow 1} \left(\frac{x^3 + 1}{x + 1} \right)$ | 8. $\lim_{x \rightarrow 0} \left(\frac{x^2 - a^2}{x^2 + 2ax + a^2} \right)$, con $x \neq -a$ |
| 4. $\lim_{x \rightarrow 3} \left(\frac{x^3 - 27}{x + 3} \right)$ | 9. $\lim_{a \rightarrow 0} \left(\frac{x^2 - a^2}{x^2 + 2ax + a^2} \right)$, con $x \neq -a$ |
| 5. $\lim_{x \rightarrow -1} \left(\frac{x^2 + 2x - 3}{x^2 - 5x + 4} \right)$ | 10. $\lim_{a \rightarrow 0} \left(\frac{x^2 - a^2}{x^2 + 2ax + a^2} \right)$, con $x \neq -a$ |

IV. Calcula el valor de los siguientes límites.

$$1. \lim_{x \rightarrow 1} \left(\frac{1-x}{x^2-1} \right)$$

$$2. \lim_{x \rightarrow -2} \left(\frac{x^3+8}{x+2} \right)$$

$$4. \lim_{x \rightarrow 1} \left(\frac{x^2-3x-4}{x^2-x-12} \right)$$

$$4. \lim_{x \rightarrow 1} \left(\frac{x-1}{x^2+3x-4} \right)$$

$$5. \lim_{x \rightarrow -3} \left(\frac{x^2-9}{x+3} \right)$$

$$6. \lim_{x \rightarrow 0} \left(\frac{x^2+4x}{3x^3+x^2-x} \right)$$

$$7. \lim_{x \rightarrow 2} \left(\frac{x^2-4x+4}{x-2} \right)$$

$$8. \lim_{x \rightarrow 2} \left(\frac{16-4x^2}{2x-4} \right)$$

$$9. \lim_{x \rightarrow 1} \left(\frac{x^2-2x+1}{x-1} \right)$$

$$10. \lim_{x \rightarrow 3} \left(\frac{x^3-27}{x-3} \right)$$

$$11. \lim_{x \rightarrow 0} \left(\frac{5x^3+4x^2-x}{x^2+x} \right)$$

V. evalúa los siguientes límites

$$1. \lim_{x \rightarrow 3} \left(\frac{x-3}{x^2-3x} \right)$$

$$2. \lim_{x \rightarrow 1} \left(\frac{x^2-2x+1}{x-1} \right)$$

$$3. \lim_{x \rightarrow -4} \left(\frac{x^2-16}{x+4} \right)$$

$$4. \lim_{x \rightarrow -1} \left(\frac{x^6-1}{x^4-1} \right)$$

$$5. \lim_{x \rightarrow 4} \left(\frac{2-\sqrt{x}}{4-x} \right)$$

$$6. \lim_{x \rightarrow 1} \left(\frac{1-\sqrt{x}}{1-\sqrt[3]{x}} \right)$$

$$7. \lim_{x \rightarrow 0} \left(\frac{\sqrt{x+1}-1}{x} \right)$$

$$8. \lim_{x \rightarrow 2} \left(\frac{1-\sqrt{x+1}}{x-2} \right)$$

$$9. \lim_{x \rightarrow 4} \left(\frac{2-\sqrt{x}}{3-\sqrt{2x+1}} \right)$$

$$10. \lim_{x \rightarrow 0} \left(\frac{1-\sqrt{1-x^2}}{x^2} \right)$$

$$11. \lim_{x \rightarrow 0} \left(\frac{1}{\sqrt{x+1}} - \frac{1}{x} \right)$$

VI. Halla el resultado de los siguientes límites

$$1. \lim_{h \rightarrow 0} \left(\frac{(x+h)^2 - x^2}{h} \right)$$

$$2. \lim_{h \rightarrow 0} \left(\frac{\frac{1}{x+h} - \frac{1}{x}}{h} \right)$$

$$3. \lim_{h \rightarrow 0} \left(\frac{\frac{1}{(x+h)^2} - \frac{1}{x^2}}{h} \right)$$

$$4. \lim_{h \rightarrow 0} \left(\frac{(x+h+2)^3 - (x+2)^3}{h} \right)$$

$$5. \lim_{x \rightarrow a} \left(\frac{\sqrt{x} - \sqrt{a} + \sqrt{x-a}}{\sqrt{x^2 - a^2}} \right), \text{ con } a \in \mathbb{R}^+$$

$$6. \lim_{h \rightarrow 0} \left(\frac{\frac{1}{\sqrt{x+h}} - \frac{1}{\sqrt{x}}}{h} \right)$$

VII. Encuentra el límite indicado

$$1. \lim_{x \rightarrow 0} \left(\frac{2}{x^2} \right)$$

$$2. \lim_{x \rightarrow 1^-} \left(\frac{1}{x^2 - 1} \right)$$

$$3. \lim_{x \rightarrow 3^-} \left(\frac{1}{x-3} \right)$$

$$4. \lim_{x \rightarrow 3^+} \left(\frac{1}{x-3} \right)$$

$$5. \lim_{x \rightarrow 0^+} \left(\frac{1}{x^2 - 2x} \right)$$

$$6. \lim_{x \rightarrow -2^-} \left(\frac{x^2}{x^2 - 4} \right)$$

$$7. \lim_{x \rightarrow -4^-} \left(\frac{x}{x+4} \right)$$

$$8. \lim_{x \rightarrow -5} \left(\frac{-1}{(x+5)^2} \right)$$

$$9. \lim_{x \rightarrow -2^-} \left(\frac{x-1}{x^2(x+2)} \right)$$

$$10. \lim_{x \rightarrow -3^+} \left(\frac{x^3}{x^2 + 5x + 6} \right)$$

$$11. \lim_{x \rightarrow 2} \left(\frac{2}{(x+2)^2} \right)$$

$$12. \lim_{x \rightarrow 1^-} \left(\frac{4x}{x-1} \right)$$

$$13. \lim_{x \rightarrow 3^-} \left(\frac{x+1}{x^2 - 9} \right)$$

$$14. \lim_{x \rightarrow 2^+} \left(\frac{5x^2}{4 - x^2} \right)$$

$$15. \lim_{x \rightarrow 1^-} \left(\frac{x+4}{x^2 - 1} \right)$$

$$16. \lim_{x \rightarrow 5^+} \left(\frac{3+x}{x-5} \right)$$

$$17. \lim_{x \rightarrow 2} \left(\frac{1}{(x-2)^2} \right)$$

$$18. \lim_{x \rightarrow 4} \left(\frac{-3}{(x-4)^2} \right)$$

$$19. \lim_{x \rightarrow 0} \left(\frac{1}{x} - \frac{1}{x^2} \right)$$

$$20. \lim_{x \rightarrow 0} \left(\frac{4x^2 - 3}{x^2 - x} \right)$$

$$21. \lim_{x \rightarrow 1^-} \left(-\frac{x}{x-1} \right)$$

$$22. \lim_{x \rightarrow -3^+} \left(\frac{4x+5}{x^2 + 3x} \right)$$

VIII. Calcula el límite

1. $\lim_{x \rightarrow 0^-} \left(\frac{\sqrt{x^2 + 4}}{x} \right)$

2. $\lim_{x \rightarrow 0^+} \left(\frac{\sqrt{x^2 + 4}}{x} \right)$

3. $\lim_{x \rightarrow 2^+} \left(\frac{\sqrt{x^2 - 1}}{x - 2} \right)$

4. $\lim_{x \rightarrow 2^-} \left(\frac{\sqrt{x^2 - 1}}{x - 2} \right)$

5. $\lim_{x \rightarrow 3} \left(\frac{1}{\sqrt{3 - x}} \right)$

6. $\lim_{x \rightarrow 3^+} \left(\frac{x}{\sqrt{x - 3}} \right)$

7. $\lim_{x \rightarrow 2^+} \left(\frac{-2}{\sqrt[3]{x - 2}} \right)$

8. $\lim_{x \rightarrow 2^-} \left(\frac{-2}{\sqrt[3]{x - 2}} \right)$

9. $\lim_{x \rightarrow 1^+} \left(\frac{x^2}{\sqrt{x + 1}} \right)$

10. $\lim_{x \rightarrow 4} \left(\frac{x^2 + 3x + 1}{(x - 4)^2} \right)$

11. $\lim_{x \rightarrow 0} \left(\frac{x^2 + x - 1}{x^3 + x^2} \right)$

12. $\lim_{x \rightarrow 0} \left(1 - \frac{1}{\sqrt{1 - x}} \right)$

IX. Calcula cada uno de los siguientes límites, si es posible.

1. $\lim_{x \rightarrow \infty} \left(\frac{3x^2 - x - 2}{5x^2 + 4x + 1} \right)$

2. $\lim_{x \rightarrow \infty} \left(\frac{2x - 3}{x + 1} \right)$

3. $\lim_{x \rightarrow \infty} \left(\frac{x + 1}{x^2 - 3x + 1} \right)$

4. $\lim_{x \rightarrow \infty} \left(\frac{2x^3 + 3x}{4x^3 - x^2 + 1} \right)$

5. $\lim_{x \rightarrow \infty} \left(\frac{x^4 - 3x^2 + 4}{x^5 + 2x^3 - x + 1} \right)$

6. $\lim_{x \rightarrow \infty} \left(\frac{5x^2 - 4x + 2}{3x - 4} \right)$

7. $\lim_{x \rightarrow \infty} \left(\frac{3x^3 - 2x^2 + 4x - 5}{x^2 - 3x + 1} \right)$

8. $\lim_{x \rightarrow \infty} \left(\frac{1}{x^2 + 2x - 1} \right)$

X. Encuentra el resultado de los siguientes límites, si es posible:

1. $\lim_{x \rightarrow -\infty} \left(\frac{3x^2 + x - 4}{5x^2 - 1} \right)$

2. $\lim_{x \rightarrow -\infty} \left(\frac{3x + 4}{x - 2} \right)$

3. $\lim_{x \rightarrow -\infty} \left(\frac{2x - 1}{4x^2 + 5x - 2} \right)$

8. $\lim_{x \rightarrow -\infty} \left(\frac{2 - x^2}{x^2 + 4x - 2} \right)$

9. $\lim_{x \rightarrow -\infty} \left(\frac{2}{x^2 - 3} \right)$

10. $\lim_{x \rightarrow -\infty} \left(\frac{5x^4 + x^3 - 1}{2x^4 - 1} \right)$

4. $\lim_{x \rightarrow -\infty} \left(\frac{x^3 - 3x^2 + x}{x - 2} \right)$

5. $\lim_{x \rightarrow -\infty} \left(\frac{3x^4 + x^3 - 2x - 4}{x^2 - x + 1} \right)$

6. $\lim_{x \rightarrow -\infty} \left(\frac{x^2 - x}{4x^3 + 5x^2 + 1} \right)$

7. $\lim_{x \rightarrow -\infty} \left(\frac{x^3 + 4x^2 + x - 1}{x^2 - 2x + 1} \right)$

11. $\lim_{x \rightarrow -\infty} \left(\frac{x^4 - 3x^2 + x}{5x^4 + 3x^3 - 2x + 1} \right)$

12. $\lim_{x \rightarrow -\infty} \left(\frac{3x^2 - 2x + 1}{1 + x - x^2} \right)$

13. $\lim_{x \rightarrow -\infty} \left(\frac{x^2 + 4x - 1}{4x + 1} \right)$

14. $\lim_{x \rightarrow -\infty} \left(\frac{3x - 1}{4x^3 - x^2 + x - 1} \right)$

XI. Determinar el resultado de cada uno de los siguientes límites.

1. $\lim_{x \rightarrow \infty} \left(\frac{\sqrt{x^2 + 1}}{x + 1} \right)$

2. $\lim_{x \rightarrow \infty} \left(\frac{\sqrt{x^2 - 2x + 3}}{x + 3} \right)$

3. $\lim_{x \rightarrow \infty} \left(\sqrt{x^2 + 2x + 4 + x} \right)$

4. $\lim_{x \rightarrow \infty} \left(\frac{-x}{\sqrt{x^2 + 1}} \right)$

5. $\lim_{x \rightarrow \infty} \left(\frac{x - 9}{\sqrt{4x^2 + 3x + 2}} \right)$

6. $\lim_{x \rightarrow \infty} \left(1 - \frac{1}{\sqrt{x^2 + 1}} \right)$

7. $\lim_{x \rightarrow \infty} \left(\frac{1 - \sqrt{x}}{1 + \sqrt{x}} \right)$

8. $\lim_{x \rightarrow \infty} \left(\frac{\sqrt{x + \sqrt{x + \sqrt{x}}}}{\sqrt{x + 4}} \right)$

XII. Encuentra, si es posible, el resultado de los siguientes límites.

1. $\lim_{x \rightarrow \infty} \left(x - \sqrt{x^2 - 4} \right)$

2. $\lim_{x \rightarrow \infty} \left(x - \sqrt{x^2 + 1} \right)$

3. $\lim_{x \rightarrow \infty} \left(x - \sqrt{x^2 - 2x + 1} \right)$

4. $\lim_{x \rightarrow \infty} \left(x - \sqrt{x^2 - 5x} \right)$

5. $\lim_{x \rightarrow \infty} \left(\sqrt{x^2 - 3} - x \right)$

6. $\lim_{x \rightarrow \infty} \left(\sqrt{x^2 + 9} - x \right)$

7. $\lim_{x \rightarrow \infty} \left(\sqrt{x^2 - 3x - x} \right)$

8. $\lim_{x \rightarrow \infty} \left(\sqrt{x^2 + 2x - x} \right)$

9. $\lim_{x \rightarrow \infty} \left(x^2 - \sqrt{x^4 - x^2} \right)$

10. $\lim_{x \rightarrow \infty} \left(x - \sqrt{x^2 - 4} \right)$

11. $\lim_{x \rightarrow \infty} \left(\sqrt{x^4 - 1} - x^2 \right)$

12. $\lim_{x \rightarrow \infty} \left(\sqrt{x^4 - x^2} - x^2 \right)$

13. $\lim_{x \rightarrow \infty} \left(\sqrt{x^4 + 5x^2 + 6} - x^2 \right)$

14. $\lim_{x \rightarrow \infty} \left(\sqrt{x^4 + 3x^2 + 2} - x^2 \right)$

15. $\lim_{x \rightarrow \infty} \left(\sqrt{x^4 - 3x^2 + x} - x^2 \right)$

16. $\lim_{x \rightarrow \infty} \left(\sqrt{x^4 - 4x^2 + 1} - x^2 \right)$

17. $\lim_{x \rightarrow \infty} \left(\sqrt{x^4 - 4x^2 + 1} - x^2 \right)$

18. $\lim_{x \rightarrow \infty} \left(\sqrt{x^4 - 3x^2 + 1} - (x + 1) \right)$

19. $\lim_{x \rightarrow \infty} \left(\sqrt{x^2 + 2x} - (x + 2) \right)$

20. $\lim_{x \rightarrow \infty} \left(\sqrt{x^4 - 4x^2 - 2} - (x^2 - 1) \right)$

XIII. Halla el valor del límite, si es posible:

$$1. \lim_{x \rightarrow \infty} (\sqrt{x^2 - 9} - \sqrt{x^2 - 1})$$

$$2. \lim_{x \rightarrow \infty} (\sqrt{x^2 - 2} - \sqrt{x^2 + 4})$$

$$3. \lim_{x \rightarrow \infty} (\sqrt{x^2 - 3x} - \sqrt{x^2 - 4})$$

$$4. \lim_{x \rightarrow \infty} (\sqrt{x^2 - 2x + 4} - \sqrt{x^2 - 6x + 3})$$

$$5. \lim_{x \rightarrow \infty} (\sqrt{x^2 - 4x + 1} - \sqrt{x^2 - 5})$$

$$6. \lim_{x \rightarrow \infty} (\sqrt{x^4 + 3x^2 - 1} - \sqrt{x^4 - x^2})$$

$$7. \lim_{x \rightarrow \infty} (\sqrt{x^4 - 2x^2 - 1} - \sqrt{x^4 - x^2 - 1})$$

$$8. \lim_{x \rightarrow \infty} (\sqrt{x^4 - 3x^2 + 1} - \sqrt{x^4 - x - 1})$$

XIV. Determina el valor de los siguientes límites, si existen, teniendo en cuenta que $(a - b)(a^2 + ab + b^2) = a^3 - b^3$

$$1. \lim_{x \rightarrow \infty} (\sqrt[3]{x^3 - 1} - x)$$

$$2. \lim_{x \rightarrow \infty} (\sqrt[3]{x^3 - 3x^2 + 1} - x)$$

$$3. \lim_{x \rightarrow \infty} (x - \sqrt[3]{x^3 + 4x^2 - x + 1})$$

$$4. \lim_{x \rightarrow \infty} ((x + 1) - \sqrt[3]{x^3 - 2})$$

$$5. \lim_{x \rightarrow \infty} (\sqrt[3]{x + 1} - \sqrt[3]{x})$$

$$6. \lim_{x \rightarrow \infty} (\sqrt[3]{x^3 - 5x^2} - \sqrt[3]{x^3 + 4})$$

$$7. \lim_{x \rightarrow \infty} (\sqrt[3]{x^3 - 2x^2} - \sqrt[3]{x^3 - 5})$$

$$8. \lim_{x \rightarrow \infty} (\sqrt[3]{x^3 - 2x^2 + 5} - \sqrt[3]{x^3 + 4x^2 + 1})$$

XV. Calcula el valor de los siguientes límites.

$$1. \lim_{x \rightarrow 0} \left(\frac{\text{sen}(5x)}{x} \right)$$

$$2. \lim_{x \rightarrow 0} \left(\frac{\text{sen}(-x)}{x} \right)$$

$$3. \lim_{x \rightarrow 0} \left(\frac{\text{sen}\left(\frac{1}{2}x\right)}{x} \right)$$

$$4. \lim_{x \rightarrow 0} \left(\frac{\text{sen}\left(\frac{2}{3}x\right)}{x} \right)$$

$$9. \lim_{x \rightarrow 0} \left(\frac{\text{sen}(\sqrt{2x})}{x} \right)$$

$$10. \lim_{x \rightarrow 0} \left(\frac{\text{sen}(\sqrt{5x})}{x} \right)$$

$$11. \lim_{x \rightarrow 0} \left(\frac{\text{sen}(-\sqrt{3x})}{x} \right)$$

$$12. \lim_{x \rightarrow 0} \left(\frac{\text{sen}\left(-\frac{\sqrt{6}}{2}x\right)}{x} \right)$$

$$5. \lim_{x \rightarrow 0} \left(\frac{\operatorname{sen}\left(\frac{5}{2}x\right)}{x} \right)$$

$$6. \lim_{x \rightarrow 0} \left(\frac{\operatorname{sen}\left(-\frac{1}{3}x\right)}{x} \right)$$

$$7. \lim_{x \rightarrow 0} \left(\frac{\operatorname{sen}\left(-\frac{3}{2}x\right)}{x} \right)$$

$$8. \lim_{x \rightarrow 0} \left(\frac{\operatorname{sen}(-4x)}{x} \right)$$

$$13. \lim_{x \rightarrow 0} \left(\frac{5\operatorname{sen}(2x)}{x} \right)$$

$$14. \lim_{x \rightarrow 0} \left(\frac{3\operatorname{sen}(-4x)}{x} \right)$$

$$15. \lim_{x \rightarrow 0} \left(\frac{\operatorname{sen}4x}{\operatorname{sen}5x} \right)$$

XVI. Calcula el resultado de los siguientes límites.

$$1. \lim_{x \rightarrow 0} \left(\frac{\operatorname{sen}(3x)}{5x} \right)$$

$$2. \lim_{x \rightarrow 0} \left(\frac{\operatorname{sen}(6x)}{4x} \right)$$

$$3. \lim_{x \rightarrow 0} \left(\frac{\operatorname{sen}(-x)}{2x} \right)$$

$$4. \lim_{x \rightarrow 0} \left(\frac{\operatorname{sen}(-3x)}{7x} \right)$$

$$5. \lim_{x \rightarrow 0} \left(\frac{\operatorname{sen}(5x)}{-x} \right)$$

$$6. \lim_{x \rightarrow 0} \left(\frac{\operatorname{sen}(6x)}{-3x} \right)$$

$$7. \lim_{x \rightarrow 0} \left(\frac{\operatorname{sen}(-4x)}{-5x} \right)$$

$$8. \lim_{x \rightarrow 0} \left(\frac{\operatorname{sen}\left(\frac{2}{3}x\right)}{-x} \right)$$

$$9. \lim_{x \rightarrow 0} \left(\frac{\operatorname{sen}\left(\frac{3}{7}x\right)}{-5x} \right)$$

$$10. \lim_{x \rightarrow 0} \left(\frac{\operatorname{sen}\left(-\frac{4}{3}x\right)}{2x} \right)$$

$$11. \lim_{x \rightarrow 0} \left(\frac{\operatorname{sen}\left(\frac{1}{3}x\right)}{\frac{6}{7}x} \right)$$

$$12. \lim_{x \rightarrow 0} \left(\frac{\operatorname{sen}\left(\frac{6}{5}x\right)}{-\frac{3}{4}x} \right)$$

XVII. Determinar el resultado de los siguientes límites.

$$1. \lim_{x \rightarrow 0} \left(\frac{\text{sen}^2(x)}{x} \right)$$

$$2. \lim_{x \rightarrow 0} \left(\frac{\text{sen}(3x)}{\text{sen}(2x)} \right)$$

$$3. \lim_{x \rightarrow 0} \left(\frac{\text{sen}(x)}{\sqrt{x}} \right)$$

$$4. \lim_{x \rightarrow 0} \left(\frac{\tan(x)}{2x} \right)$$

$$5. \lim_{x \rightarrow 0} \left(\frac{2\text{sen}(x) - \text{sen}(2x)}{x \cos(x)} \right)$$

$$6. \lim_{x \rightarrow 0} \left(\frac{\text{sen}(2x)\cos(x)}{3x} \right)$$

XVIII. Encontrar el valor de cada límite

$$1. \lim_{x \rightarrow 0} (\cos(x))$$

$$2. \lim_{x \rightarrow 0} \left(\frac{3 \tan^2(x)}{x^2} \right)$$

$$3. \lim_{x \rightarrow 0} (\text{sen}(x+a))$$

$$4. \lim_{x \rightarrow 0} (\cos(x+a))$$

$$5. \lim_{x \rightarrow a} (\text{sen}(x))$$

$$6. \lim_{x \rightarrow a} (\cos(x))$$

$$7. \lim_{x \rightarrow 0} \left(\frac{1 - \cos(4x)}{x} \right)$$

$$8. \lim_{x \rightarrow 0} \left(\frac{1 - \cos(x)}{1 + \text{sen}(x)} \right)$$

$$9. \lim_{x \rightarrow 0} \left(\frac{1 - \cos(2x)}{4x} \right)$$

$$10. \lim_{x \rightarrow 0} \left(\frac{3x^2}{1 - \cos^2\left(\frac{1}{2}x\right)} \right)$$

$$11. \lim_{x \rightarrow 0} \left(\frac{1 - \cos^2(x)}{2x^2} \right)$$

$$12. \lim_{x \rightarrow 0} \left(\frac{\tan^4 x}{4x^4} \right)$$

$$13. \lim_{x \rightarrow 0} \left(\frac{1 - \cos(2x)}{\text{sen}(3x)} \right)$$

$$14. \lim_{x \rightarrow 0} \left(\frac{\text{sen}(4x)}{\cos(3x) - 1} \right)$$

$$15. \lim_{x \rightarrow 0} \left(\frac{x^2 + 3x}{\text{sen}(x)} \right)$$

$$16. \lim_{x \rightarrow 0} \left(\frac{\text{sen}(x)}{3x^2 + 2x} \right)$$

$$17. \lim_{x \rightarrow 0} \left(\frac{x}{\text{sen}(3x)} \right)$$

$$18. \lim_{x \rightarrow 0} \left(\frac{x^2}{1 - \cos(x)} \right)$$

$$19. \lim_{x \rightarrow 0} \left(\frac{1 - \cos(3x)}{\text{sen}(3x)} \right)$$

$$20. \lim_{x \rightarrow 0} \left(\frac{1 - \cos^2(x)}{x} \right)$$

$$21. \lim_{x \rightarrow 0} \left(\frac{4x}{\tan(x)} \right)$$

$$22. \lim_{x \rightarrow 0} \left(\frac{\csc(3x)}{2 \cot(x)} \right)$$

$$23. \lim_{x \rightarrow 0} \left(\frac{2x^2 - 3x}{2\text{sen}(x)} \right)$$

$$24. \lim_{x \rightarrow 0} (\tan(x))$$

XI X. Encontrar el valor de cada límite

1. $\lim_{x \rightarrow 0} \left(\frac{\operatorname{sen}^2(x)}{1 + \cos^3(x)} \right)$

2. $\lim_{x \rightarrow 0} \left(\frac{1 - \cos(2x)}{\operatorname{sen}(3x)} \right)$

3. $\lim_{x \rightarrow 0} \left(\frac{\tan(2x)}{\operatorname{sen}(x)} \right)$

4. $\lim_{x \rightarrow \pi} \left(\frac{\operatorname{sen}(x - \pi)}{x - \pi} \right)$

5. $\lim_{x \rightarrow 1} \left(\frac{\operatorname{sen}(x^2 - 1)}{x - 1} \right)$

6. $\lim_{x \rightarrow 0} \left(\frac{1 - \cos(2x)}{x^2} \right)$

7. $\lim_{x \rightarrow 0} \left(\frac{\cos(2x) - \cos(4x)}{x^2} \right)$

8. $\lim_{x \rightarrow 0} \left(\frac{\operatorname{sen}(2x)\cos(x)}{3x} \right)$

9. $\lim_{x \rightarrow \pi} \left(\frac{\operatorname{sen}(mx)}{\operatorname{sen}(mx)} \right)$

10. $\lim_{x \rightarrow -1} \left(\frac{\operatorname{sen}(x+1)}{x^2 - 1} \right)$

11. $\lim_{x \rightarrow 3} \left(\frac{x^2 - 6x + 9}{\operatorname{sen}^2(x-3)} \right)$

12. $\lim_{x \rightarrow 0} \left(\frac{\operatorname{sen}(\operatorname{sen}(x))}{x} \right)$

13. $\lim_{x \rightarrow 0} \left(\frac{\sec(x) - 1}{x \sec(x)} \right)$

14. $\lim_{x \rightarrow \frac{\pi}{3}} \left(\frac{1 + \cos(2x)}{x} \right)$

15. $\lim_{x \rightarrow 0} \left(\frac{\tan(2x)}{\frac{x}{2}} \right)$