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Choose T (true) or F (false) for each statement.

1. The partial fraction decomposition of the integral $\int \frac{4x^2+5x-45}{x^3-2x^2-15x} dx$ is $\frac{A}{x} + \frac{B}{(x+3)} + \frac{C}{(x-5)}$

F

2. The integral of $\int \frac{5x^2+20x+6}{x^3+2x^2+x} dx$ is $6 \ln|x| - \ln|x+1| - 9 \ln|x+1| + C$

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V

3. The integral of $\int (18-12x)(x^2-3x)^2 dx$ is $-2(x^2-3x)^4 + C$

V

4. The integral of $\int 5x\sqrt{x-3} dx$ is $(x-3)^{\frac{5}{2}} + (x-3)^{\frac{3}{2}} + C$

V

5. Solve the following integral, **THE STEPS OF YOUR PROCEDURE.**

$$\int \frac{x^3 - 3x^2 + 1}{x^2 - 1} dx$$

$$\int \frac{x^3 - 3x^2 + 1}{(x+1)(x-1)} dx = \frac{3/2}{(x+1)} - \frac{1/2}{(x-1)} = \frac{3}{2} \ln|x+1| - \frac{1}{2} \ln|x-1| + C$$

1/2

$$\frac{A}{(x+1)} + \frac{B}{(x-1)}$$

$$A(x-1) + B(x+1) = x^3 - 3x^2 + 1$$

$x=1 \quad x=-1$

$$\frac{3}{2}x = A$$

$$x = \frac{1}{2} - \frac{1}{2} = \frac{0}{2}$$

$$\frac{x^3 - 3x^2 + 1}{2} = \frac{3}{2} \ln|x+1| - \frac{1}{2} \ln|x-1| + C$$

CORRECTION:

$$\begin{array}{r} x-3 \\ x^2-1 \overline{) x^3-3x^2+0x+1} \\ \underline{-x^3+0+x} \\ -3x^2+x+1 \\ \underline{+3x^2+0-3} \\ x-2 \end{array}$$

$$\int \frac{x^3-3x^2+1}{x^2-1} dx = (x-3) + \frac{x-2}{(x+1)(x-1)} = (x-3) + \frac{3/2}{(x+1)} - \frac{1/2}{(x-1)}$$

$$A+B(1) = 1-2$$

$$B(2) = -1$$

$$B = -1/2$$

$$(x-3) + \frac{x-2}{x^2-1}$$

$$A(-1) = -1-2$$

$$A(-2) = -3$$

$$A = 3/2$$

$$\frac{A}{(x+1)} + \frac{B}{(x-1)}$$

$$A(x-1) + B(x+1)$$

$x=1 \quad x=-1$

$$= \frac{x^2}{2} - 3x + \frac{3}{2} \ln|x+1| - \frac{1}{2} \ln|x-1| + C$$

$$0 + B(1+1) = (1)^3 - 3(1)^2 + 1$$

$$B(2) = 1 - 3 + 1$$

$$B(2) = -1$$

$$B = -1/2$$

$$A(-1-1) + 0 = (-1)^3 - 3(-1)^2 + 1$$

$$A(-2) = -1 - 3 + 1$$

$$A(-2) = -3$$

$$A = 3/2$$

$$\begin{aligned} & 1) x^3 - 2x^2 - 15x \\ & x(x^2 - 2x - 15) \\ & x(x-5)(x+3) \end{aligned}$$



$$2) \frac{5x^2 + 20x + 6}{x^3 + 2x^2 + x} = \frac{5x^2 + 20x + 6}{x(x+1)(x+1)}$$

$$\begin{aligned} & x(x^2 + 2x + 1) \\ & x(x+1)(x+1) \end{aligned}$$

$$\frac{A}{x} + \frac{B}{x+1} + \frac{C}{x+1}$$

$$A(x+1)(x+1) + B(x)(x+1) + C(x)(x+1)$$

$$x = -1 \quad x = 0$$

$$Ax^2 + A2x + A2 + Bx^2 + Bx + Cx^2 + Cx$$

$$x^2(A+B+C) + x(2A+B+C) + 2A$$

$$A+B+C = 5$$

$$2A+B+C = 20$$

$$2A = 6$$

$$A = 3$$

$$3) \int (18 - 12x)(x^2 - 3x)^2 dx \quad \int \frac{6(x^2 - 3x)^3}{3} = -2(x^2 - 3x)^3 + C$$

$$u = x^2 - 3x$$

$$du = 2x - 3$$

$$4) \int 5x\sqrt{x-3} dx = \int 5(u+3)u^{1/2} du = \int (5u + 15)u^{1/2} du = \int 5u^{3/2} + 15u^{1/2} du = \int \frac{5u^{5/2}}{5/2} + \frac{15u^{3/2}}{3/2} = 2u^{5/2} + 10u^{3/2}$$

$$u = x-3 \quad x = u+3 \quad \frac{u}{2} \rightarrow \frac{5}{2} = \frac{10}{2} = 2 \quad \frac{15}{2} \rightarrow \frac{3}{2} = \frac{30}{2} = 15$$

$$du = 1 \quad dx = du$$

$$= 2(x-3)^{5/2} + 10(x-3)^{3/2} + C$$

EXERCISES

1. $\int \frac{1}{x^2} dx = \int x^{-2} dx = \frac{x^{-1}}{-1} = -\frac{1}{x} + C$

2. $\int \frac{1}{x^3} dx = \int x^{-3} dx = \frac{x^{-2}}{-2} = -\frac{1}{2x^2} + C$

3. $\int \frac{1}{x^4} dx = \int x^{-4} dx = \frac{x^{-3}}{-3} = -\frac{1}{3x^3} + C$

4. $\int \frac{1}{x^5} dx = \int x^{-5} dx = \frac{x^{-4}}{-4} = -\frac{1}{4x^4} + C$

5. $\int \frac{1}{x^6} dx = \int x^{-6} dx = \frac{x^{-5}}{-5} = -\frac{1}{5x^5} + C$

6. $\int \frac{1}{x^7} dx = \int x^{-7} dx = \frac{x^{-6}}{-6} = -\frac{1}{6x^6} + C$

7. $\int \frac{1}{x^8} dx = \int x^{-8} dx = \frac{x^{-7}}{-7} = -\frac{1}{7x^7} + C$

8. $\int \frac{1}{x^9} dx = \int x^{-9} dx = \frac{x^{-8}}{-8} = -\frac{1}{8x^8} + C$

9. $\int \frac{1}{x^{10}} dx = \int x^{-10} dx = \frac{x^{-9}}{-9} = -\frac{1}{9x^9} + C$

10. $\int \frac{1}{x^{11}} dx = \int x^{-11} dx = \frac{x^{-10}}{-10} = -\frac{1}{10x^{10}} + C$