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Introduction

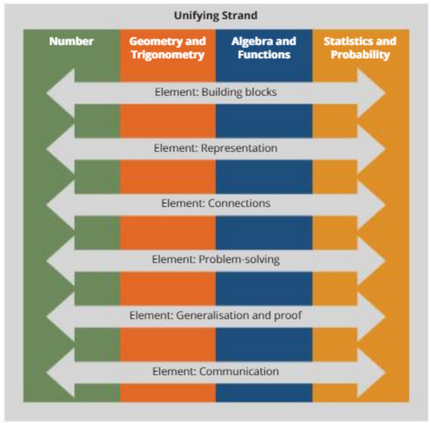
This new edition of *Active Maths 1* is a comprehensive three-year textbook covering the complete Junior Cycle Maths Ordinary Level specification. After finishing *Active Maths 1*, Higher Level students can continue the Junior Cycle Higher Level course with *Active Maths 2*.

The subject of maths covers many different areas and on completion of this book you will be able to:

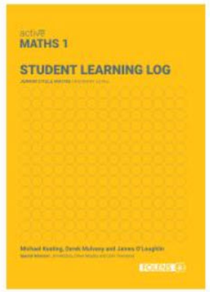
- Grasp mathematical concepts
- Carry out mathematical procedures efficiently and accurately
- Formulate and solve maths problems
- Think logically, reflect on your thoughts and explain your reasoning to others
- See how useful maths is when applied to the world you live in

Active Maths 1 fully covers the entire Junior Cycle Ordinary Level specification.

1. **The Unifying Strand**. This strand permeates the whole book. There is no specific content within it, rather the learning outcomes are applicable to the content of the four other strands.
2. **Number**
3. **Geometry and Trigonometry**
4. **Algebra and Functions**
5. **Statistics and Probability**



- A separate free Learning Log encourages further investigation of a specific topic within each chapter and also provides you with an opportunity to reflect on your own learning. This is an integral part of the Junior Cycle key skills you are expected to develop as a student.



We have worked hard to improve the quality of this new book and believe that those who use it will enjoy and absorb all that the new Junior Cycle Maths specification has to offer.

Michael Keating, Jim McElroy, Derek Mulvany, Oliver Murphy, James O'Loughlin and Colin Townsend

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