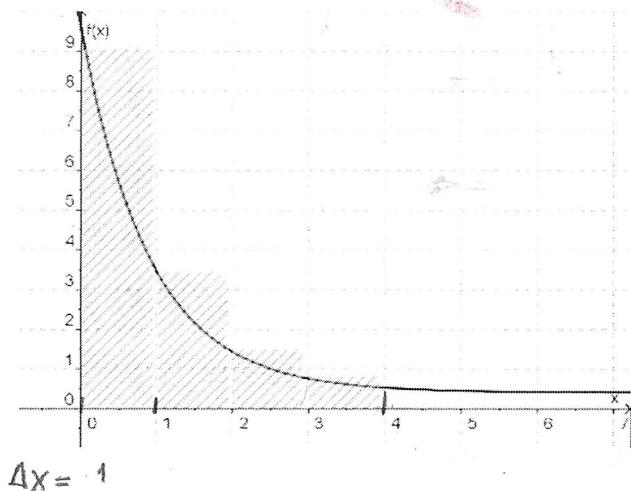


Name Hannia Yanisa Gómez Wolfskill I.D. A01570193 March, 2017

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**I. Multiple choice. Choose the letter of the right answer (10 points).**

1. Choose the sentence that best describes the approximate area below the graph of  $f(x)$ :



- a) Approximation of the area on the interval  $[0, 4]$  using 4 partitions with left-hand calculations.
- b) Approximation of the area on the interval  $[1, 5]$  using 4 partitions with right-hand calculations.
- c) Approximation of the area on the interval  $[0, 4]$  using 4 partitions with right-hand calculations.
- d) Approximation of the area on the interval  $[1, 5]$  using 4 partitions with left-hand calculations.

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**II. Evaluate the integral using the following values. SHOW THE STEPS OF YOUR PROCEDURE. (5 points each)**

$\int_2^4 x dx = 9$        $\int_2^4 x^3 dx = 54$        $\int_2^4 dx = 7$

- a.  $\int_2^4 (5x^3 + 4x + 6) dx = \frac{348}{}$  ✓
- b.  $\int_2^4 23 dx = \frac{161}{}$  ✓
- c.  $\int_5^5 x^3 dx = \frac{0}{}$  ✓
- d.  $\int_4^2 x dx = \frac{-9}{}$  ✓

**IV. Procedure. Solve the following problem showing your entire procedure.**

1) Approximate the area of a plane regions using left hand, right hand and middle points approximations.

$f(x) = 9 - x^2$  on  $[3, 5]$  4 rectangles (20 points)

$\Delta x = \frac{5-3}{4} = 0.5$

Area (Left hand) =  $\frac{-10.75 u^2}{}$  ✓  
Area (Right hand) =  $\frac{-18.75 u^2}{}$  ✓

- $(0.5)f(3) = 0$
- $(0.5)f(3.5) = -1.625$
- $(0.5)f(4) = -3.5$
- $(0.5)f(4.5) = -5.625$
- $(0.5)f(5) = -8$
- $(0.5)f(4.5) = -5.625$
- $(0.5)f(4) = -3.5$
- $(0.5)f(3.5) = -1.625$