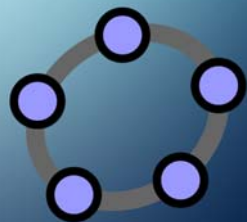


中學數學電子學習系列：(2) 在數學課堂有效運用資訊科技 (進階程度)

教育局數學教育組

2019 年 4-5 月



GeoGebra 簡介

- GeoGebra 是為了小學到大學的教學而設計的開源 (open source) 動態數學軟體。
- GeoGebra 是一套結合幾何 (平面+立體)、代數、統計及微積分等的免費動態幾何軟件，它是在 2001 年由 Markus Hohenwarter 在奧地利的 Salzburg 薩爾茨堡大學所設計。
 - GeoGebra 其實就是他的碩士論文。
 - 目前在奧地利 Linz 的 Johannes Kepler 大學 (克卜勒大學) 擔任數學教學研究所所長。
- GeoGebra 是由 Java 寫成的，因此可以跨平台使用。
- GeoGebra 的一些學與教用途：
 - 教師用於課堂演示互動幾何圖像；
 - 學生用於探索與發現幾何概念，猜想幾何定理。
- 2011: [38 developers](#) & 200 translators Celebrating 10 years of GeoGebra



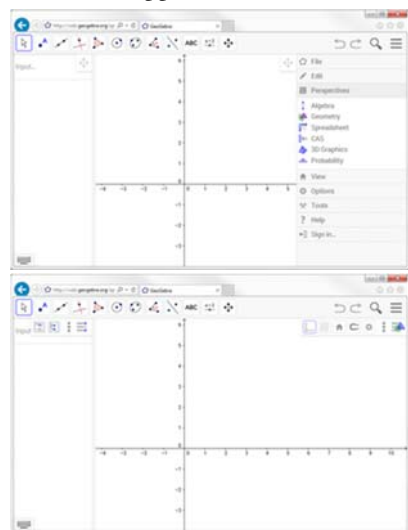
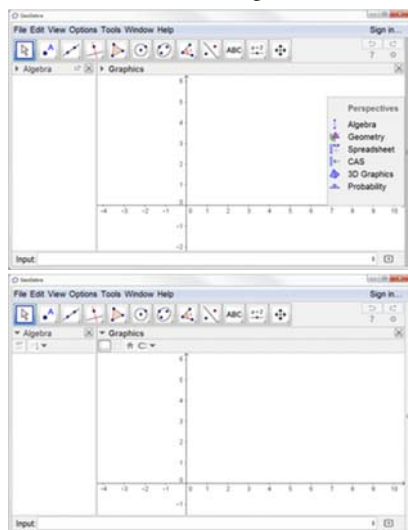
*If you want to go fast, go alone.
If you want to go far, go together.*

最近版本： 6.0.529

Stable release 6.0.452.0 (8 April 2018)
Stable release: 6.0.518 (20 December 2018)
<https://en.wikipedia.org/wiki/GeoGebra>

下載與安裝

- GeoGebra Desktop 桌機版 vs. Web and Tablet App 線上版或平板版



GeoGebra 經典 6



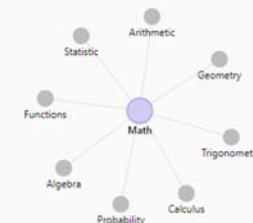
GeoGebra 經典 5

GeoGebra: Books

- **Mathematical Modeling: Applications with GeoGebra**
 - Hall, J., Lingefjärd T. (2016). *Mathematical Modeling: Applications with GeoGebra*. New York: Wiley. [568 pages]
- **GeoGebra - 幾何與代數的美麗邂逅**
 - 羅驥韋 (2013)。《GeoGebra 幾何與代數的美麗邂逅》。臺北市：五南。

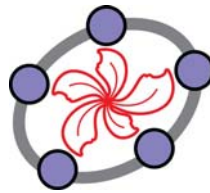
GeoGebra: Resources

- Find over 1 million free activities, simulations, exercises, lessons, and games for math & science!
 - <https://www.geogebra.org/materials>
 - <https://www.geogebra.org/t/math>
 - <https://www.geogebra.org/m/bgmn44x5>
- **Tutorials:**
 - <https://wiki.geogebra.org/en/Tutorials>
 - <https://www.geogebra.org/a/14>



GeoGebra: Resources

- GeoGebra Institutes
 - <https://www.geogebra.org/institutes>
- GeoGebra Institute of Hong Kong (GIHK)
 - <http://www.geogebra.org.hk>
- Applets in Tablets: GeoGebra 數學電子教室
 - <https://www.gmath.hk/>
 - <http://www.geogebra.hk/>
 - <http://www.geogebra.hk/reference>
- (Learning GeoGebra from Examples)
<https://www.geogebra.org/m/FZFjhBaa>
- (Graph Plotter 2018)
<https://www.geogebra.org/m/wQthUaaa>



5

*How GeoGebra (and other IT tools)
may enrich classroom L&T?*

Mathematics Education Section

6

Advantages of GeoGebra

- Dynamic
- Extremely rich in functions
- Fast to observe and conclude

7

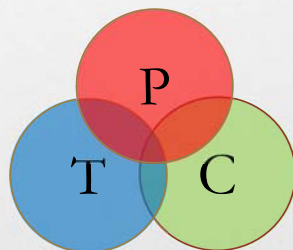
Disadvantages of GeoGebra

- Dynamic **without knowing the mechanisms**
- **Too** rich in functions **without knowing the focus**
- **Too** fast to observe and conclude **only by superficial observations**

8

Key question

- What to teach?
- How to use?
- How to **refine**?



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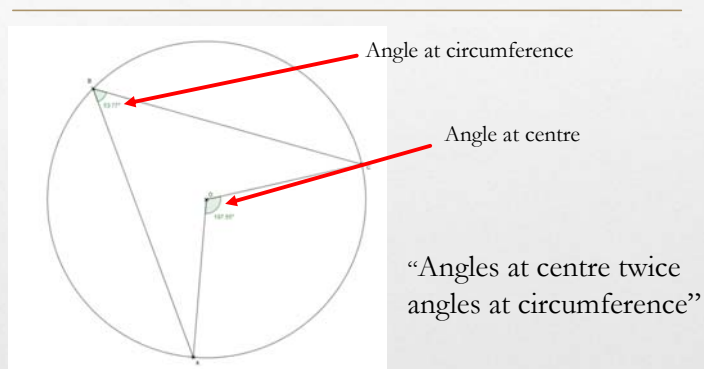
L&T in Properties of Circles

- A refinement process on L&T package using dynamic geometry software
- A theorem on the properties of circles



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The theorem



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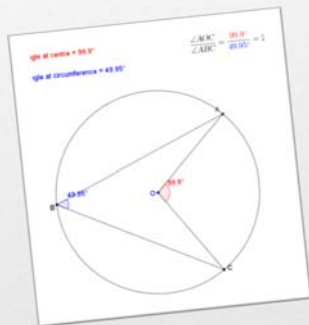
The proof Does it work?

A collage of images related to the proof of the theorem. It includes a diagram of a circle with a central angle and an inscribed angle, with text labels: "Angle at centre = $\angle AOC = 132.2^\circ$ ", "Angle at circumference = $\angle ABC = 66.1^\circ$ ", " $\angle AOC = 132.2^\circ = 2 \times \angle ABC = 2 \times 66.1^\circ$ ". There is a thought bubble containing the text "Pedagogical considerations?", another thought bubble containing "How can a task aim at the difficulties?", and a third thought bubble containing "What are students' difficulties?". A statue of The Thinker is shown in the bottom right corner. A question mark is shown in the bottom left corner.

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Refinement: From visualisation to abstraction

Understand the limitations



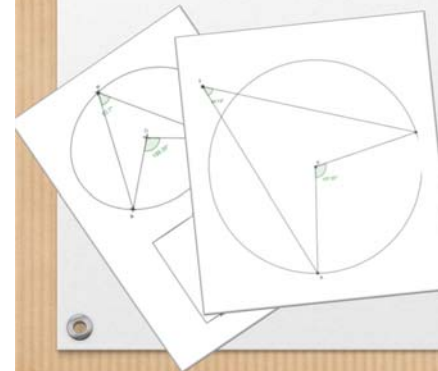
Dynamic geometry vs Euclidean Geometry?

Computation work vs Mind work

13

Refinement: From visualisation to abstraction

Stretch the potential



Re-reading a geometric theorem:

In a circle, an angle at any points of the circumference is half of the angle subtended by the same arc of the circle at the centre.

Conditions and consequences:

Pedagogy of variations

14

A complete cycle of teaching

- Examples versus verifications
- Counter-examples versus constraints

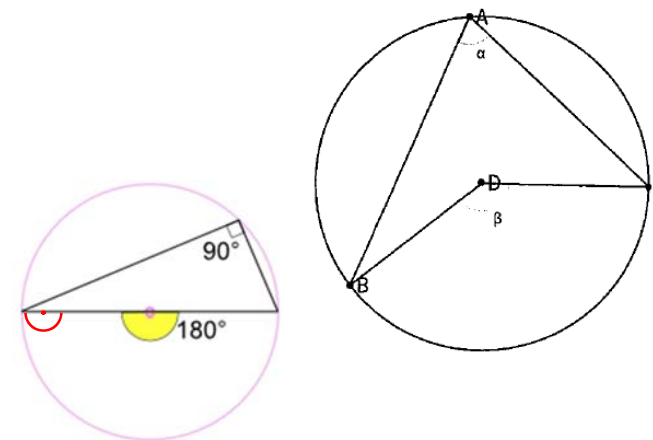
15

Re-visit the theorem: Think about it

Section D: Think about it

Question 2

Cody claims that if $\beta = 2\alpha$, D must be the centre of the circle. Do you agree? Explain your answer.



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