## PABSON SEE PRE BOARD EXAM - 2077 (PC231)

Time: 3:00 hrsOptional MathematicsF.M. : 100Candidates are required to write their answers according to the<br/>instructions given.

Attempt all questions.

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**Group**"A"  $5 \times (1+1) = 10$ 

- 1. (a) Define constant function with an example.
  - (b) If 3, a, 27 and 81 are in G.P., find the value of a.
- 2. (a) What is the point of discontinuity of a function  $f(x) = \frac{x+1}{x-1}$ ?
  - (b) Find the value of k if  $\begin{vmatrix} 4 & 1+k \\ 6 & 5 \end{vmatrix} = \begin{vmatrix} 2 & 4 \\ k & 3 \end{vmatrix}$
- 3. (a) If the lines  $a_1x + b_1y + c_1 = 0$  and  $a_2x + b_2y + c_2 = 0$  are parallel to each other, then show that  $a_1b_2 = a_2b_1$ .
  - (b) If the intersection plane is parallel to the axis of cone then what conic does it form?
- 4. (a) Write the formula for  $2 \sin A \cdot \sin B$ .
  - (b) Solve:  $3 \tan^2 \theta 1 = 0 \ [0^\circ \le \theta \le 90^\circ]$
- 5. (a) If  $\vec{a} = \vec{i} 2\vec{j}$  and  $\vec{b} = -6\vec{i} 3\vec{j}$ , then prove that  $\vec{a}$  is perpendicular to  $\vec{b}$ .
  - (b) If a point P(-4, 3a 5) has its image P'(7 a, 4) under the reflection in the line y = -x, find the value of a.

Group"B"

 $[13 \times 2 = 26]$ 

- 6. (a) If g(x+5) = x+20 then find g(x) and gog(x).
  - (b) If  $x \sqrt{2}$  is a factor of  $ax^3 6x + 2\sqrt{2}$ , then find the value of a.
  - (c) What is the common difference of an AP whose first term and sum of first 15 terms are 100 and 450 respectively?

- 7. (a) If  $P = \begin{bmatrix} 2 & -1 \\ -4 & 5 \end{bmatrix}$  and  $Q = \begin{bmatrix} -3 \\ 3 \end{bmatrix}$ , find the matrix R such that PR = Q.
  - (b) According to Cramer's rule, find the values of  $D_x$  and  $D_y$  for x + y = 5 and x y = 3.
- 8. (a) If the acute angle between two straight lines 2x y + 6 = 0and 3x + ky + 4 = 0 is 45°, find the value of k.
  - (b) Show that the lines  $y + \sqrt{3}x + 4 = 0$  and  $x \sqrt{3}y = 5$  are perpendicular to each other.
- 9. (a) Prove :  $\cot 2A + \tan A = \operatorname{cosec} 2A$ 
  - (b) Prove:  $2\cos 105^\circ \cdot \cos 15^\circ + \frac{1}{2} = 0$
  - (c) Solve:  $\tan^2 \frac{\theta}{3} \frac{2}{\sqrt{3}} \tan \frac{\theta}{3} + \frac{1}{2} = 0.$
- 10. (a) If  $\vec{a} + \vec{b} + \vec{c} = 0$ ,  $|\vec{a}| = 6$ ,  $|\vec{b}| = 7and|\vec{c}| = \sqrt{127}$ , find the angle between  $\vec{a}$  and  $\vec{b}$ .
  - (b) In  $\triangle ABC$ ,  $\overrightarrow{OA} = 2\vec{i} + 3\vec{j}$ ,  $\overrightarrow{OB} = \vec{i} 2\vec{j}$  and position vector of centroid G of  $\triangle ABC$  is  $\overrightarrow{OG} = 3\vec{i} + 4\vec{j}$ , then find  $\overrightarrow{OC}$ .
  - (c) In a data, the first quartile and the quartile deviation are 17.5 and 20 respectively. Find the third quartile and the co-officient of quartile deviation.
    - **Group"C"**  $[11 \times 4 = 44]$
- 11. Solve:  $3x^3 13x^2 + 16 = 0$
- 12. The sum of three numbers in AP is 18. If 1, 2 and 7 are added to them respectively, the numbers will be in G.P., then find the numbers.

$$f(x) = \begin{cases} x+2 & \text{if } 1 \le x < 0\\ 3x-2 & \text{if } x \ge 2 \end{cases}$$

Then,

- (a) Find f(x) if x = 1.99.
  (b) Find f(x) if x = 2.01.
  (c) Is lim <sub>x→2<sup>-</sup></sub> f(x) = lim <sub>x→2<sup>+</sup></sub> f(x) ?
  (d) Is f(x) continuous at x = 2?
- 14. Solve by matrix method:  $4x \frac{9}{y} + 11 = 0$  and  $\frac{6}{y} 3x = 8$ .
- 15. Find the single equation of the pair of straight lines passing through (3, -1) and perpendicular to the pair of lines represented by  $x^2 xy 2y^2 = 0$ .
- 16. Prove that:

$$\sin^4 \frac{\pi^c}{8} + \sin^4 \frac{3\pi^c}{8} + \sin^4 \frac{5\pi^c}{8} + \sin^4 \frac{7\pi^c}{8} = \frac{3}{2}$$

17. If  $A + B + C = \pi^c$  then prove that:

$$\frac{\cos A}{\sin B \cdot \sin C} + \frac{\cos B}{\sin C \sin A} + \frac{\sin C}{\sin A \sin B}$$

- 18. A ladder of length 20 feet is leaned on the top of a wall which makes an angle of 60° with the ground. The ladder slides 7.32 feet below the top along the wall, find the new angle that the ladder makes with ground.
- 19. Find the inversion point of the given point A(5,4) with respect to the circle  $x^2 + y^2 6x 4y + 9 = 0$ .
- 20. Find the mean deviation from median and its coefficient from the following frequency table.

Marks	$0 \le x < 10$	$10 \le x < 20$	$20 \le x < 30$	$30 \le x < 40$	$40 \le x < 50$
Number of students	5	2	9	2	2

21. Compute standard deviation and it's coefficient from the the following data.

Marks	0 - 10	0 - 20	0 - 30	0 - 40	0 - 50
Number of students	9	15	19	31	40
. Gr	$[4 \times 5 = 20]$				

- 22. Maximize and minimise the the objective function F = 6x + 5ysubject to the constraints  $x + y \le 6, x - y \ge -2, x \ge 0$  and  $y \ge 0$ .
- 23. Find the the equation of a circle with centre (3,2) and passing through the centre of the circle  $x^2 + y^2 2x + 4y 4 = 0$ .
- 24. Prove by vector method that the midpoint of hypotenuse of a right angle triangle is equidistant from its vertices.
- 25. E denotes enlargement [(0,0),2] and R denotes the reflection on the the line y = -x. If  $\Delta PQR$  with vertices P(-4,6), Q(-6,-10) and R(12,-8) mapped to form  $\Delta P''Q''R''$  under the enlargement EoR then find the coordinates of  $\Delta P''Q''R''$  and plot the the triangles on the same graph