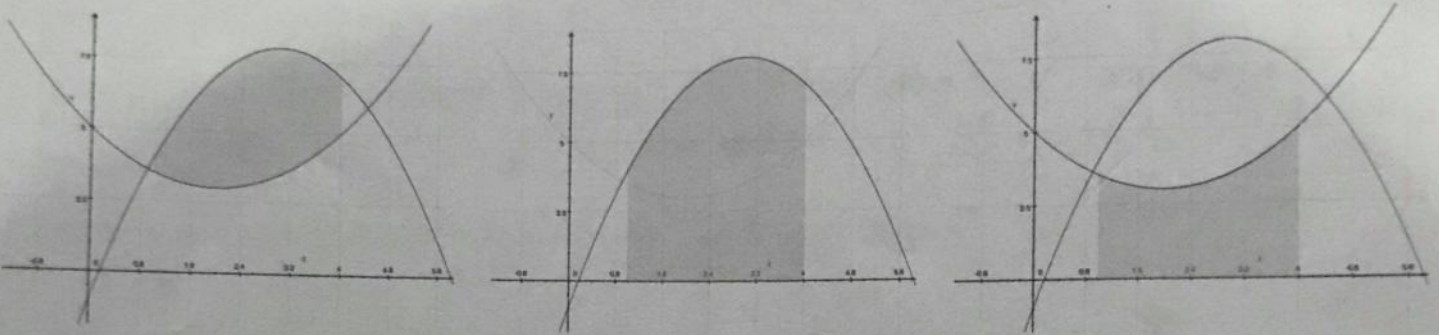


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Activity 4.3: Area between two curves

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Area between two graphs

$$\int_a^b [f(x) - g(x)] dx$$

=

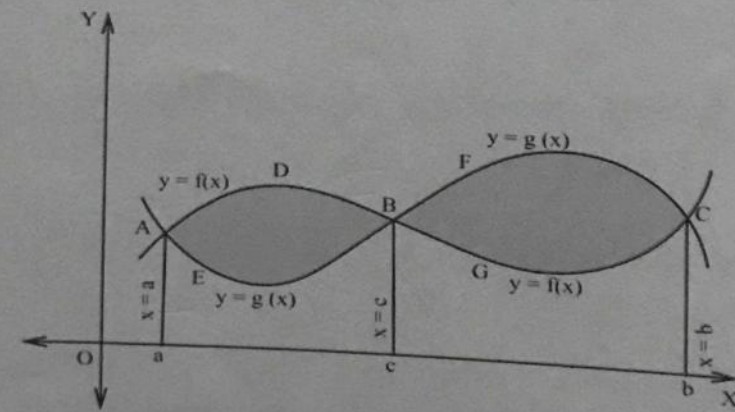
Area below  $f(x)$

$$\int_a^b f(x) dx$$

-

Area below  $g(x)$

$$\int_a^b g(x) dx$$



Source: <http://silverbullet.in/chapters/lessonsummary/3442/3250>, retrieved on July 1st, 2016

$$A_1 = \int_a^c [f(x) - g(x)] dx$$

$$A_2 = \int_c^b [g(x) - f(x)] dx$$

Determine the area between the two given functions, limited by the given vertical lines  $x = a$  and  $x = b$ . REMEMBER to graph!

1. Determine the area limited by curves  $g(x) = \frac{1}{2}x + 4$ , and  $f(x) = x^2 + 2x + 1$ , and lines  $x = -2$  and  $x = 1$

$$\int_{-2}^1 (\frac{1}{2}x + 4 - x^2 - 2x - 1) dx = \int_{-2}^1 (-x^2 - \frac{3}{2}x + 3) dx = \left[ -\frac{x^3}{3} - \frac{3}{4}x^2 + 3x \right]_{-2}^1 = 8.25 \text{ u}^2$$

2. Determine the area limited by the curves  $g(x) = -x$  and  $f(x) = x^2 + 2$ , and lines  $x = 0$  and  $x = 1$

$$\int_0^1 (x^2 + 2 + x) dx = A = \left[ \frac{x^3}{3} + \frac{2x^2}{2} + 2x \right]_0^1 = 2.83 \text{ u}^2$$

3. Determine the area limited by curves  $g(x) = 2 + x$  and  $f(x) = 1 - x^2$ , and lines  $x = 0$  and  $x = 1$

$$\int_0^1 (2 + x - 1 + x^2) dx = \int_0^1 (1 + x + x^2) dx = A = \left[ x + \frac{x^2}{2} + \frac{x^3}{3} \right]_0^1 = 1.83 \text{ u}^2$$

4. Determine the area limited by curves  $g(x) = x + 2$  and  $f(x) = x^2$

$$\int_0^1 (x + 2 - x^2) dx = A = \left[ \frac{x^2}{2} + 2x - \frac{x^3}{3} \right]_0^1 = 4.5 \text{ u}^2$$

5. Determine the area limited by the curves  $g(x) = x^2$  and  $f(x) = \sqrt{x}$

$$\int_0^1 (x^2 - x^{\frac{1}{2}}) dx = A = \left[ \frac{x^3}{3} - \frac{2}{3}x^{\frac{3}{2}} \right]_0^1 = \frac{1}{3} \text{ u}^2$$

6. Determine the area limited by the curves  $g(x) = 2x + 5$  and  $f(x) = x^2 + 2x + 1$ , and lines  $x = -2$  and  $x = 2$

$$\int_{-2}^2 (2x + 5 - x^2 - 2x - 1) dx = \int_{-2}^2 (-x^2 + 4) dx = A = \left[ -\frac{x^3}{3} + 4x \right]_{-2}^2 = 10.67 \text{ u}^2$$

7. Determine the area limited by the curves  $g(x) = \sin(x)$  and  $f(x) = \cos(x)$ , and lines  $x = \frac{\pi}{4}$  and  $x = \frac{5\pi}{4}$

$$\int_{\frac{\pi}{4}}^{\frac{5\pi}{4}} (\sin(x) - \cos(x)) dx = A = [-\cos(x) - \sin(x)]_{\frac{\pi}{4}}^{\frac{5\pi}{4}} = 2.83 \text{ u}^2$$

8. Determine the area limited by the curves  $g(x) = \frac{1}{2}x + 2$  and  $f(x) = x^2$ , and lines  $x = -1$  and  $x = 1$

$$\int_{-1}^1 (\frac{1}{2}x + 2 - x^2) dx = A = \left[ \frac{x^2}{4} + 2x - \frac{x^3}{3} \right]_{-1}^1 = 3.33 \text{ u}^2$$

9. Determine the area of the region between the graphs of  $f(x) = 3x^3 - x^2 - 10x$  and  $g(x) = -x^2 + 2x$

$$\int_0^2 (3x^3 - x^2 - 10x + x^2 - 2x) dx = \int_0^2 (3x^3 - 12x) dx = A = \left[ \frac{3x^4}{4} - 6x^2 \right]_0^2 = 24 \text{ u}^2$$

10. Determine the area limited by curves  $g(x) = e^{\frac{x}{2}} + 2$  and  $f(x) = 3 - 2x$ , and lines  $x = -1$  and  $x = 1$

$$\int_{-1}^1 (3 - 2x - e^{\frac{x}{2}} + 2) dx = A = \left[ 5x - x^2 - 2e^{\frac{x}{2}} \right]_{-1}^1 = 1.21 \text{ u}^2$$

$$\int_{-1}^1 (e^{\frac{x}{2}} + 2 - 3 + 2x) dx = A = \left[ 2e^{\frac{x}{2}} - x + x^2 \right]_{-1}^1 = 2.507 \text{ u}^2$$

Additional practice:

<http://cdn.kutasoftware.com/Worksheets/Calc/07%20-%20Area%20Between%20Curves.pdf>

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