Sets Review

Ms. Duffy

Day 1 Notation Subsets

Note: Answers to practice questions are in red

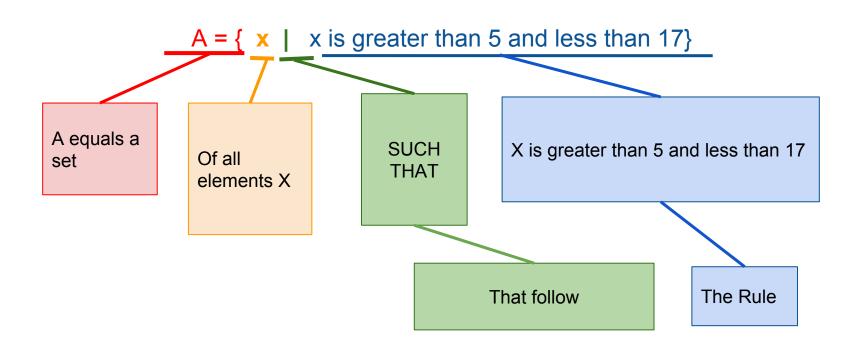
What is a set?

A **set** is a <u>clearly defined</u> collection.

What are elements?

The items in a set are referred to as the **elements** of a set.

$A = \{x \mid x \text{ is greater than 5 and less than 17}\}$



Set Notation

Writing out the rule

- Capital letter to name the set
- Open curly brackets
- X | X is ...
- Make sure rule clearly defines the set
- Close curly brackets

 $A = \{ x \mid x \text{ is a natural number less than 5} \}$

Writing out the elements

- Capital letter to name the set
- Open curly brackets
- Commas to separate elements
- Close curly brackets

$$A = \{4, 3, 2, 1\}$$

$$c = \{x \text{ is a whole number}\}$$

$$c = \{x \text{ is a whole number}\}$$

$$C = \{ x \mid x \text{ is a whole number} \}$$

$$M = \{x \mid 4, 5, 6, 7\}$$

$$M = \{x \mid 4, 5, 6, 7\}$$

$$M = \{ 4, 5, 6, 7 \}$$

$$A = x \mid x \text{ is an even number}$$

$$A = x \mid x \text{ is an even number}$$

 $A = \{ x \mid x \text{ is an even number} \}$

$$b = \{x \mid x \text{ is a whole number greater than 5, less than 9} \}$$

 $B = \{ x \mid x \text{ is a whole number greater than 5, less than 9} \}$



This symbol means "is an element of"

$$5 \in A$$

5 is an element of A

Œ

This symbol means "is not an element of"

7 ∉ A

7 is NOT an element of A

null set (or empty) set is

a set that contains NO elements

Example: The set of the names of people in the world taller than 4 metres.

Ø or {}

The symbol for the null set (or empty) set

Ø or {}

When are two sets equal?

Two sets are equal only if they contain the EXACT same elements.

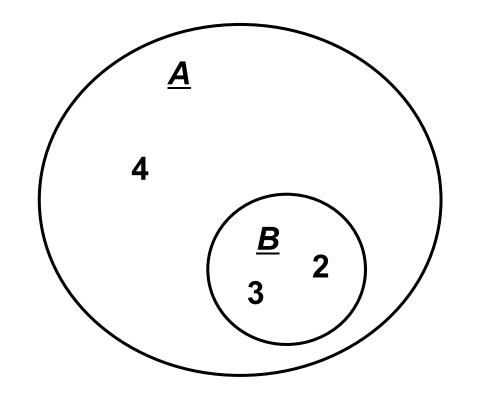
Breakdown the word

Sub Set

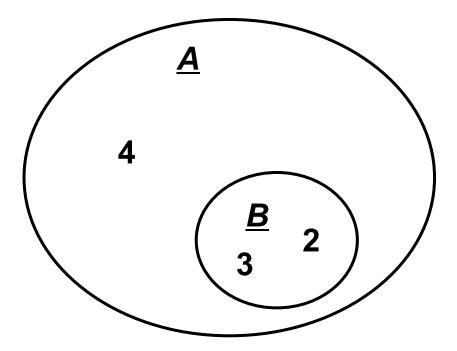
What does "sub" mean?

Sub- | snb, səb | prefix

- 1 at, to, or from a lower level or position: subalpine.
 - lower in rank: subaltern | subdeacon.
 - of a smaller size; of a subordinate nature: subculture. SUB SET = Smaller Set
- 2 somewhat; nearly; more or less: subantarctic.
- 3 denoting subsequent or secondary action of the same kind: sublet | subdivision.
- 4 denoting support: subvention.
- 5 Chemistry in names of compounds containing a relatively small proportion of a component: suboxide.



You can think of a **subset** as a set that "fits inside" of another set.



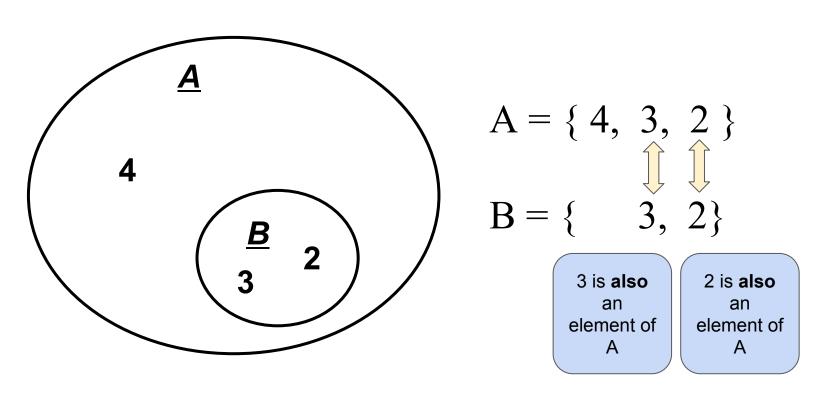
** Only write each element once **

3 is an element of A and B2 is an element of A and B4 is only an element of A

$$A = \{ 4, 3, 2 \}$$

 $B = \{ 3, 2 \}$

Set B is a **subset** of Set A if every element of B is **also** an element of A.



ALL elements in the subset can match to elements in the larger or equal set.

$$A = \{ 4, 3, 2 \}$$
 $B = \{ 3, 2 \}$

Is a subset always smaller?

Set B is a subset of Set A if every element of B is also an element of A.

$$A = \{ 1, 2, 3 \}$$

$$B = \{1, 2, 3\}$$

Set B is a subset of Set A if

every element of B is also an element of A.

Justify which box contains a set and its subset.

A

 $M = \{4, 3, 2\}$

 $N = \{ 7, 3, 2 \}$

B

$$L = \{ 0, 3, 9 \}$$

$$P = \{ 3, 9, 0 \}$$

Justifying Your Ideas Properly

Restate what you are justifying

Box B contains a set and its subset because every element of L is also an element of P.

Use "because"

Give the reason the statement is true

Create three subsets that fit inside of Set B.

 $B = \{3, 5, 7, 9, 11, 13, 15, 17\}$

Any answer that ONLY uses the elements in B is correct.

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Example answer:

C = \{3, 5\}

D = \{3\}

E = \{3, 5, 7\}
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Create three subsets that fit inside of Set B.

 $B = \{3, 5, 7, 9, 11, 13, 15, 17\}$

Why is $M = \{3, 4, 5\}$ not a subset of B?

M is not a subset of B because not every element of M can be found in B.

OR

M is not a subset of B because there is an element in M that is not in B.

Translates to "is a subset of"

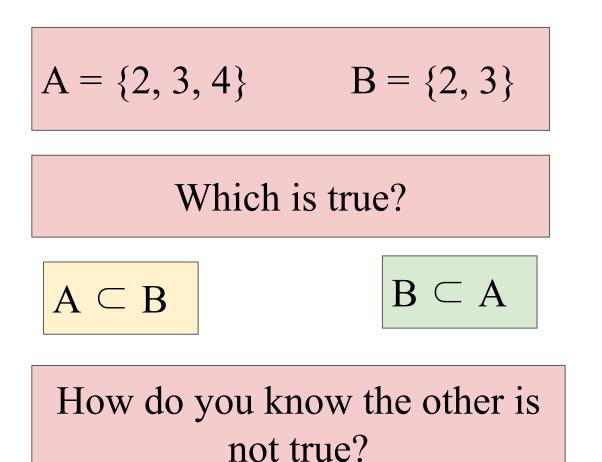
$A \subseteq B$

A "is a subset of" B

 $B \subseteq A$

B "is a subset of" A

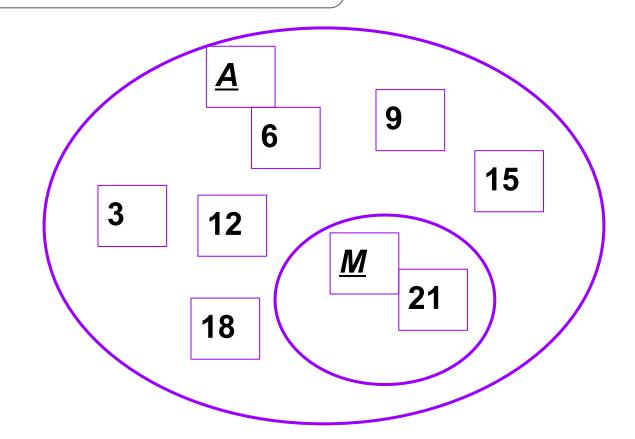
Translates to "is NOT a subset of"



 $B \subseteq A$ is true B is a subset of A. We know B is a subset of A because every element of B can be found in A.

 $A \subseteq B$ is not true because A is not a subset of B. A is not a subset of B because every element of A cannot be found in B.

List the elements of A and the elements of M.



$A = \{3, 6, 9, 12, 15, 18, 21\}$

 $M = \{21\}$

$$M = \{4, 8, 12, 16\}$$

 $N = \{2, 4\}$
 $O = \{12, 16\}$

Which of the following is true? How do you know?

a. M = N

b. O ⊂ Nc. N ⊄ M

Justify why the other two options are not true.

 $O \subseteq N$ is not true because every element of O cannot be found N.

M = N is not true because M and N do not have exactly the same elements.

$N \not\subseteq M$ is true because N is not a subset of M. N is not a subset of M because not every element of N can be found in M.

List the elements of Sets B and K.

 $B = \{x \mid x \text{ is an even, natural number greater than 17 and less than 25}\}$

 $K = \{x \mid x \text{ is a lowercase letter of the English alphabet in print that a curve is always used to make}\}$

Ex. p has a curve in it x does not have a curve in it

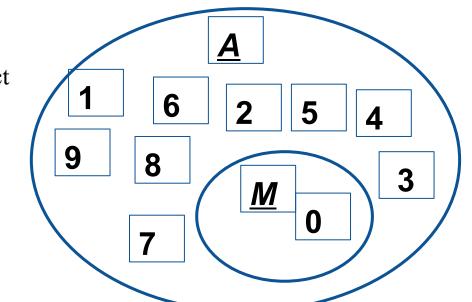
$B = \{18, 20, 22, 24\}$

 $K = \{a, b, c, d, e, f, g, j, o, p, q, r, s, u\}$

True or False?

If false, make the expression true using correct set notation.

- $1.3 \in A$ $2.0 \in A$
 - $3.7 \notin A$
- $4. M \in A$
- $5.9 \notin A$
- $6.A \notin M$
- 7. What could be a rule for Set A? Express it, using proper set notation.
- 8. What could be a rule for Set M? Express it, using proper set notation.

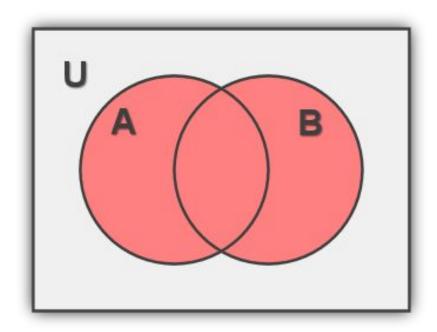


- 1. True
- 2. True
- 3. False. 7 is an element of A.
- 4. False. M is a subset of A.
- 5. False. 9 is an element of A.
- 6. False. A is not a subset of M.
- 7. A possible rule for set A could be the set of integers greater than -1 and less than 10.
- 8. A possible rule for M is the set of integers that cannot be a denominator in a fraction.

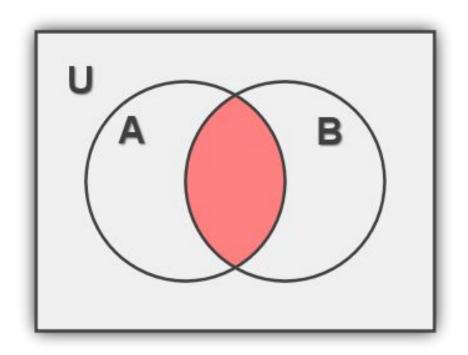
Day Two Union and Intersection Cardinality Complement

Visualising Union and Intersection

Shade the Venn Diagram to represent Union.



Shade the Venn Diagram to represent Intersection.



The **intersection** of two sets is the set of elements in common to both.



$$\cap$$
 = "intersect"

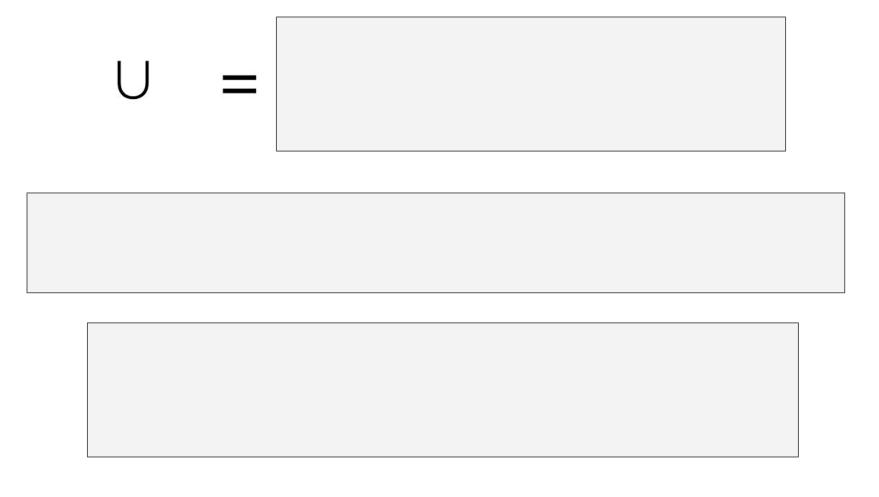
$$A \cap B =$$

= "intersect"

 $A \cap B = A "intersect" B$

The **union** of two sets A and B is found by putting together in a new set all of the elements of A and B

** Only write each element once **



 \cup = "union"

* just think \cup for \cup nion

$$\cup$$
 = "union"

* just think \cup for \cup nion

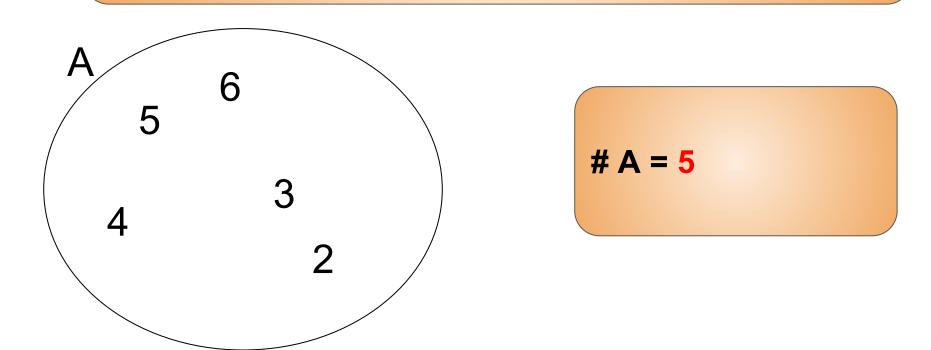
$$A \cup B =$$

 \cup = "union"

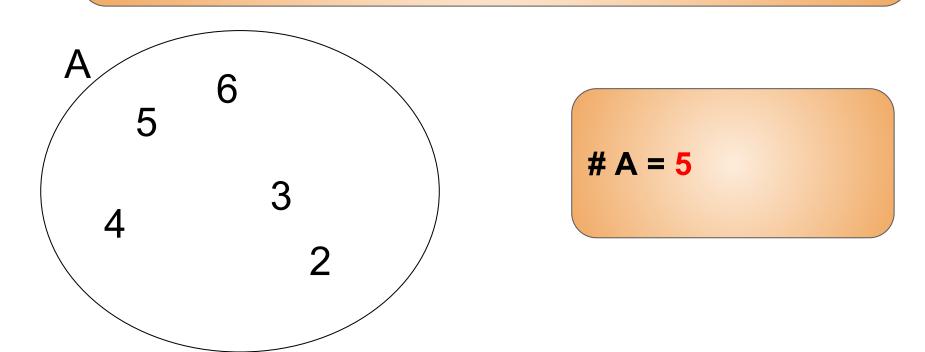
* just think \cup for \cup nion

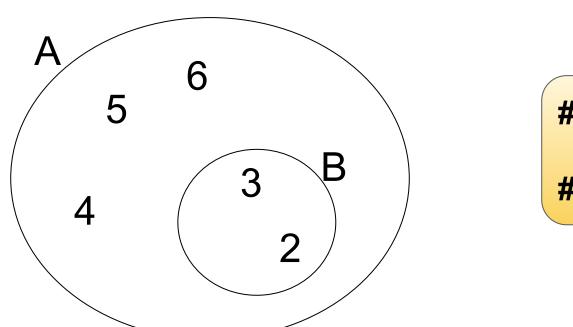
 $A \cup B = A$ "union" B

Symbol is a hashtag # A = number of items in A

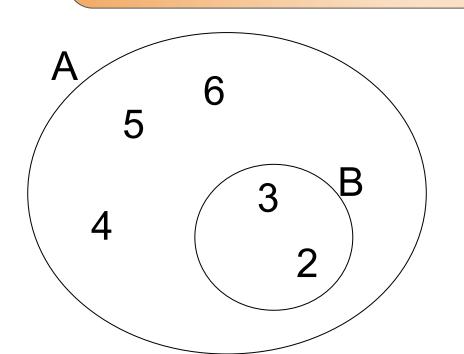


Symbol is a hashtag # A = number of items in A





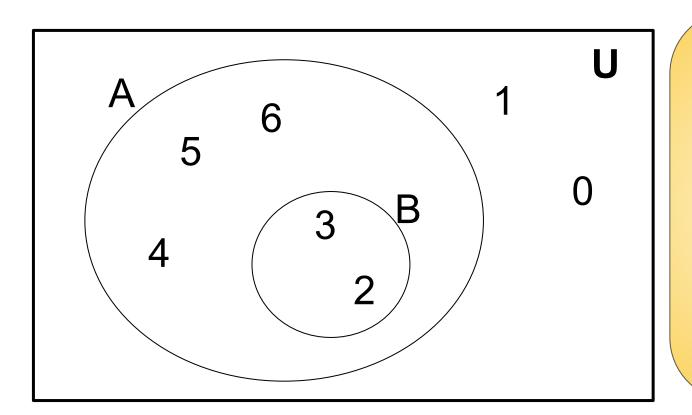




$$\# A = 5$$

$$\#B=2$$

Complement of A refers to the set of items NOT in A

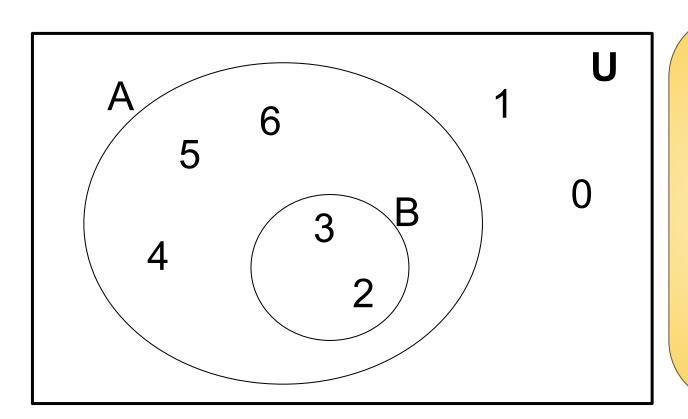


The symbol for finding the complement is an apostrophe.

A' = the set of everything NOT in A

A' =

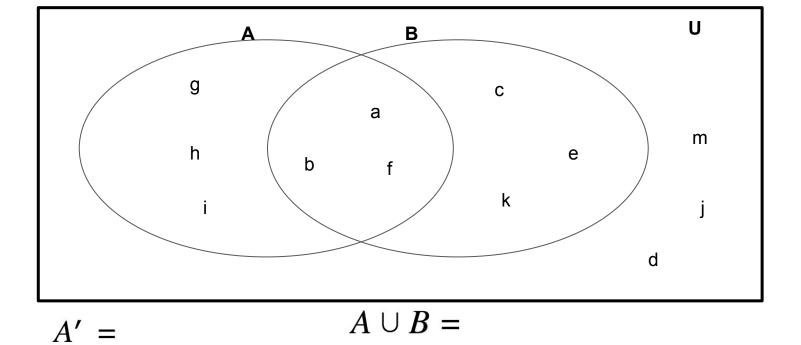
Complement of A refers to the set of items NOT in A



The symbol for finding the complement is an apostrophe.

A' = the set of everything NOT in A

$$A' = \{3, 2\}$$



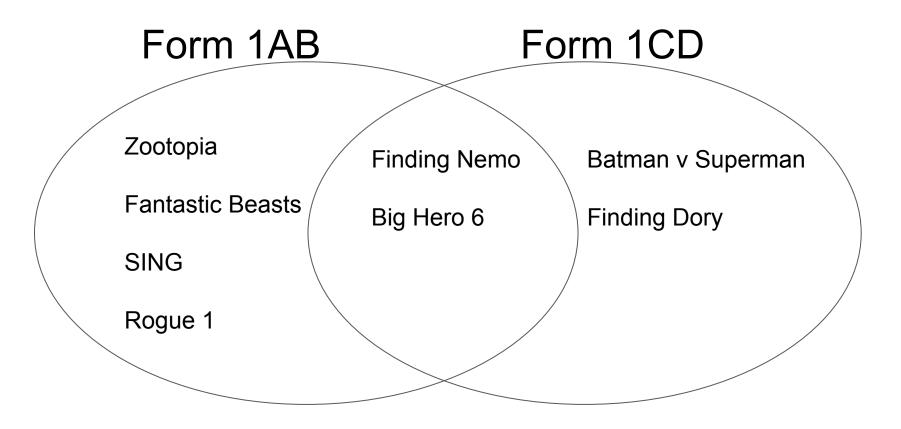
$$A = \prod_{i \in \mathcal{B}} A_i$$

 $A \cap B =$

$$\#A = (A \cup B)' =$$

 $\#(A\cap B)=$

The forms top favorite movies



How would you describe where *Big Hero 6* and *Finding Nemo* are? How would you describe where Batman vs Superman and Finding Dory are? Put the following sets into the Venn Diagram.

$$U = \{2, 4, 6, 8, 10, 12, 14, 16, 18, 20\}$$

$$C = \{x \mid x \text{ is a multiple of 4}\}$$

$$H = \{x \mid x \text{ is a multiple of 3}\}$$

