

Natural Logarithm Function 3/10/17

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$$1- y = \frac{\ln 3x}{\ln 3x}$$

$$u = \frac{3}{x} \quad u' = \frac{3}{x^2} = \frac{3}{x^2} \cdot \frac{1}{x} = \frac{3}{3x^3} = \frac{1}{x^3}$$

$$\frac{(\ln 3x) \left(\frac{1}{x} \right) - (\ln 3x)' \left(\frac{1}{x} \right)}{(\ln 3x)^2} = \frac{\ln 3x - \frac{1}{x} \cdot \frac{1}{x^3}}{(\ln 3x)^2}$$

$$2- f(x) = \sqrt{1 + \ln x}$$

$$f'(x) = (1 + \ln x)^{-1/2} = \frac{1}{\sqrt{1 + \ln x}} \cdot \frac{1}{x}$$

$$= \frac{1}{2x \sqrt{1 + \ln x}}$$

$$3- h(x) = \ln(e^x)$$

$$e^x = (e^x) \quad \lim_{x \rightarrow \infty} \frac{e^x}{e^x} = 1$$

Scribo



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Find the derivative of the following functions: **BOX YOUR FINAL ANSWER**

1) $f(x) = 4x^3(2x + 5)^2$
 $= (2x^2(3x + 5))^2 = 30x^2(3x + 5)^2$

2) $f(x) = (4x + 1)(3 - x)^2$
 $= (3 - x)^2(4x + 1) + (4x + 1)(2(3 - x)(-1))$

3) $f(x) = \left(\frac{x}{2} + 1\right)(x^2 - 3)^2$
 $= \left(\frac{x}{2} + 1\right)(2(x^2 - 3)(2x)) + (x^2 - 3)^2(1)$

4) $f(x) = \frac{2x^2}{(x^2 + 1)^2}$
 $= \frac{(2x)(2x) + (2x^2)(-2)(x^2 + 1)(2x)}{(x^2 + 1)^4}$

5) $f(x) = \frac{8x}{x + 1} - \frac{6(x + 1) - 6x}{(x + 1)^2}$
 $= \frac{8x(x + 1) - (6(x + 1) - 6x)(x + 1)^2}{(x + 1)^3}$

6) $f(x) = \frac{(2x - 3)^2}{1 - 2x}$
 $= \frac{(2x - 3)^2(1 - 2x) + (2x - 3)^2(-2)(1 - 2x)^2}{(1 - 2x)^3}$

7) $f(x) = \frac{(2x - 3)^2}{1 - 2x}$
 $= \frac{(2x - 3)^2(1 - 2x) + (2x - 3)^2(-2)(1 - 2x)^2}{(1 - 2x)^3}$

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10) $f(x) = \frac{(2x - 3)^2}{1 - 2x}$
 $= \frac{(2x - 3)^2(1 - 2x) + (2x - 3)^2(-2)(1 - 2x)^2}{(1 - 2x)^3}$

11) $f(x) = \frac{(2x - 3)^2}{1 - 2x}$
 $= \frac{(2x - 3)^2(1 - 2x) + (2x - 3)^2(-2)(1 - 2x)^2}{(1 - 2x)^3}$

12) $f(x) = \frac{(2x - 3)^2}{1 - 2x}$
 $= \frac{(2x - 3)^2(1 - 2x) + (2x - 3)^2(-2)(1 - 2x)^2}{(1 - 2x)^3}$

13) Find the equation of tangent line to the given function at the indicated point:
 $f(x) = x(2x - 3)^2$ at $x = 1$

14) Find the equation of tangent line to the given function at the indicated point:
 $f(x) = \frac{(2x - 1)^2}{x}$ at $x = 1$

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*Responde simplificados
atras.

#Procedure on the book

$$4x(3x-1)^4$$

$$6x-8+15$$

$$4x(2x-1)^4 [21x-8]$$

(a)

$$3(1-2x)^4 [-4x - (1-2x)^2]$$

$$= 4x - 4x^2 + 4x - 1$$

$$3(1-2x)^4 [-4x^2 - 1]$$

$$48x^4 - 96x^3 + 72x^2 - 24x + 3 [-4x^2 - 1]$$

$$-96x^3 + 72x^2 - 24x + 3 [-4x^2 - 1]$$

$$3(-32x^3 + 24x^2 - 8x + 17) [-4x^2 - 1]$$

$$3 \cdot 2x^4(1-x)^2 [5(1-x)^2 - 3x]$$

$$2x^4(1-x)^2 [5 - 8x]$$

$$(-x+1)(-x+1)$$

$$2x^4(x^2 - 2x + 1)$$

$$8x^6 - 4x^5 + 2x^4$$

$$4(3x-7)^3 [3x - 3x + 7]$$

$$14(3x-7)^2$$

$$4(3x-7)^3 [7]$$

x⁵



More on rules of derivatives
By: Derivative rules

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- If $f(x) = 1$, $f'(x) = 6$, $g(x) = -3$, $f'(x) = 2$. Find the values of
 - $(f \cdot g)'(x) = f'(x)g(x) + f(x)g'(x) = 2(-3) + 1(-6) = -12$
 - $(f/g)'(x) = \frac{f'(x)g(x) - f(x)g'(x)}{(g(x))^2} = \frac{-12 - (-6)}{9} = \frac{-6}{9} = -\frac{2}{3}$
 - $(g/f)'(x) = \frac{g'(x)f(x) - g(x)f'(x)}{(f(x))^2} = \frac{-6(1) - (-3)(2)}{1} = -6 + 6 = 0$
- If $f(x) = 4$, $g(x) = 2$, $f'(x) = -6$ and $g'(x) = 5$, find the following values
 - $(f+g)'(x) = f'(x) + g'(x) = -6 + 5 = -1$
 - $(f-g)'(x) = f'(x) - g'(x) = -6 - 5 = -11$
 - $(f \cdot g)'(x) = f'(x)g(x) + f(x)g'(x) = -6(2) + 4(5) = -12 + 20 = 8$
 - $(f/g)'(x) = \frac{f'(x)g(x) - f(x)g'(x)}{(g(x))^2} = \frac{-12 - 20}{4} = \frac{-32}{4} = -8$

If $h(x) = f(x)g(x)$, use the table to find $h'(1)$, $h'(0)$ and $h'(5)$

x	f(x)	f'(x)	g(x)	g'(x)
-1	2	1	1	2
0	-1	0	-1	3
1	2	-1	0	5

$$h'(x) = f'(x)g(x) + f(x)g'(x)$$

$$h'(0) = (-1)(0) + (-1)(3) = -3$$

$$h'(1) = (0)(1) + (2)(5) = 10$$

If $h(x) = \frac{f(x)}{g(x)}$, use the table to find $h'(1)$, $h'(0)$ and $h'(5)$

x	f(x)	f'(x)	g(x)	g'(x)
-1	2	1	1	2
0	-1	0	-1	3
1	2	-1	2	5

$$h'(1) = \frac{f'(1)g(1) - f(1)g'(1)}{(g(1))^2} = \frac{-1(2) - (2)(5)}{2^2} = \frac{-2 - 10}{4} = \frac{-12}{4} = -3$$

$$h'(0) = \frac{f'(0)g(0) - f(0)g'(0)}{(g(0))^2} = \frac{0(-1) - (-1)(3)}{(-1)^2} = \frac{0 - (-3)}{1} = 3$$

$$h'(5) = \frac{f'(5)g(5) - f(5)g'(5)}{(g(5))^2} = \frac{-1(2) - (2)(5)}{2^2} = \frac{-2 - 10}{4} = -3$$