

95
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I. Circle the right answer. (5 point each)

1) Find the slope for $f(x) = -5x^2$ at $x=3$

- A) 30 B) -75 C) -45 D) -30

$(3, -45)$
 $f'(x) = -10x$
 $f'(3) = -30$
 $y - y_1 = m(x - x_1)$
 $y - 45 = -30(x - 3)$
 $y = -30x + 90 + 45$
 $y = -30x + 135$

2) What is the equation of the tangent line for the curve $y = x^3 + 2$ at the point $(-1, 1)$

- A) $y = -3x + 4$ B) $y = 3x - 4$ C) $y = 3x + 4$ D) $y = -3x - 4$

$f(x) = x^3 + 2$
 $f'(-1) = 3(-1)^2 = 3$
 $f'(-1) = 3$
 $y - 1 = 3(x + 1)$
 $y = 3x + 3 + 1$
 $y = 3x + 4$

3) The following functions is not differentiable at $x = -4$

- a) $f(x) = |x + 4|$ b) $f(x) = x^2 - 4$ c) $f(x) = \frac{x+2}{x-4}$ $f(x) = \sqrt{-x+4}$

4) The following function is not differentiable at $x = 1$

- a) $f(x) = \frac{1}{x+1}$ b) $y = (x-1)^{1/2}$ c) $f(x) = |x+1|$ d) $f(x) = \sqrt[3]{x-1}$

II. Answer the following questions.

1. The position of an object, s , at any time, t , is given by: (15 points)

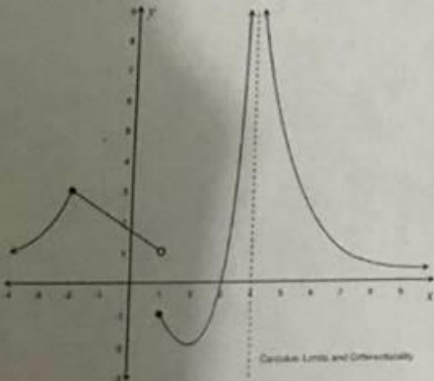
$s(t) = -18t^3 + 15t + 8$ where s is measured in feet and t is measured in seconds.

Find the equation of acceleration at any time $a(t)$.

$s(t) = -54t^2 + 15$ $v'(t) = a(t)$ $a(t) = -108t$

$s'(t) = v(t)$ $v(t) = -54t^2 + 15$ $v'(t) = -108t$

2. The following graph shows the function $y = f(x)$ (20 points)



- a) Find the values of "x" where the function is not continuous $x = 1, x = 2$
 b) Find the values of "x" where the function is not differentiable $x = -2, x = 1, x = 4$

III. Find the derivative by definition of the following function: (15 points)

$$f(x) = 3x^2 + 5 \quad f'(x) = 6x$$

$$f'(x) = \lim_{h \rightarrow 0} \frac{3(x+h)^2 + 5 - (3x^2 + 5)}{h}$$

$$f'(x) = \lim_{h \rightarrow 0} \frac{3(x^2 + 2xh + h^2) + 5 - (3x^2 + 5)}{h}$$

$$f'(x) = \lim_{h \rightarrow 0} \frac{3x^2 + 6xh + 3h^2 + 5 - 3x^2 - 5}{h}$$

$$f'(x) = \lim_{h \rightarrow 0} \frac{h(6x + 3h)}{h}$$

$$f'(x) = 6x + 3(0)$$

$$f'(x) = 6x$$

IV. Find the derivative of the following:

a) $f(x) = 8\sqrt{x^3} - 2x^3 + \frac{5}{x^2}$ (10 points)

$$f(x) = 8x^{3/2} - 2x^3 + 5x^{-2}$$

$$f'(x) = 6x^{1/2} - 6x^2 - 10x^{-3}$$

$$f'(x) = \frac{6}{\sqrt{x}} - 6x^2 - \frac{10}{x^3}$$

b) $f(x) = 2(1-3x^2)^5 + \sqrt{4x-1}$ (10 points)

$$f(x) = 2(1-3x^2)^5 + (4x-1)^{1/2}$$

$$f'(x) = 10(1-3x^2)^4(-6x) + \frac{1}{2}(4x-1)^{-1/2}(4)$$

$$f'(x) = -60x(1-3x^2)^4 + \frac{2}{\sqrt{4x-1}}$$

c) $f(x) = 7(4x-5x^2)^6$ (10 points)

$$f(x) = 7(4x-5x^2)^6$$

$$f'(x) = 42(4x-5x^2)^5(4-15x)$$

$$f'(x) = 42(4-15x)(4x-5x^2)^5$$

1



$$f(x) = \sqrt[3]{x-1}$$



2

