

CALCULUS II
FIRST PARTIAL

QUIZ 1A

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Answer the following problems with complete procedure.

1. Find the approximate value of $(3.04)^3$ (20 pts)

-15

$$\Delta x = .04$$

$$f(x) = x^3$$

$$f'(x) = 3x^2$$

$$m = 3$$

$$x_2 = 3.04$$

$$dy = 3(3)^2 \cdot .04 = 27 \cdot .12 = 3.24$$

Calculator ≈ 28.009

$$f(x + \Delta x) = f(x) + f'(x) \Delta x$$

2. Given the equation $f(x) = x^2 - 2x + 3$ find the line tangent to the curve at $x = a = 0$. (20 pts)

-5

$$f(0) = 0^2 - 2(0) + 3 = 3$$

$$x = 0$$

$$y = 3$$

$$f'(x) = 2x - 2 = m = -2$$

evaluate $x = 0$

$$y - 3 = (2x - 2)(x - 0)$$

$$y - 3 = 2x^2 - 2x$$

$$y = 2x^2 - 2x + 3$$

Not a straight line!

3. The edge of a cube was found to be 20 cm. with a possible error in measurement of 0.1 cm. Estimate the maximum possible error in computing the volume of the cube (20 pts)

-15

$$\Delta x = .1 \text{ cm}$$

$$x_1 = 20$$

$$x_2 = 20.1$$

$$V = 20^3 \approx 8,000 \text{ cm}^3$$

$$dV = 3x^2 \cdot \Delta x$$

$$dV = 3(20)^2 \cdot .1 = 1200$$

$$V = 8000 \text{ cm}^3 \pm 1200 \text{ cm}^3$$

Determine if the following... $\int (\sin x + \cos x) dx$ is $-\cos(x) + \sin(x) + C$

4. A can is going to be modified in such a way that its height will change from 14cm to 14.8 cm but the diameter of the base will remain as 9cm.

a) Find the change in the volume of the can (20 pts)

$x_1 = 14 \rightarrow \Delta x = 0.8$
 $x_2 = 14.8$

$V_1 = \pi (4.5)^2 (14) = 890.64 \text{ cm}^3$
 $V_2 = \pi (4.5)^2 (14.8) = 941.53 \text{ cm}^3$
 $\Delta V = 50.89 \text{ cm}^3$

b) Find the approximate change in the volume of the can (20 pts)

$dy = f'(x) \Delta x = dV = \pi (4.5)^2 (0.8) = 50.8938 \text{ cm}^3 = dy$
 $f'(x) = \pi r^2$

3. The edge of a cube was found to be 30 cm with a possible error in measurement of 0.5 cm. Find the maximum possible error in computing the volume of the cube.

Find the approximate value of $(3.04)^3$

$$\Delta x = .04$$

$$f(x) = x^3$$

$$f'(x) = 3x^2$$

$$x_1 = 3$$

$$x_2 = 3.04$$

$$f(x + \Delta x) = f(x) + f'(x) \Delta x$$

$$= 3^3 + (3(3)^2)(.04)$$

$$= 27 + 1.08$$

$$= \boxed{28.08}$$

Given the equation $f(x) = x^2 - 2x + 3$ find the line tangent to the curve at $x = a = 0$

$$x = 0 \quad f(0) = 0^2 - 2(0) + 3 = 3$$

$$y = 3 \quad y - 3 = -2(x - 0)$$

$$y = -2x + 3$$

$$f'(x) = 2x - 2$$

$$f'(0) = 2(0) - 2$$

$$f'(0) = -2 = m$$

The edge of a cube was found to be 20 cm with a possible error in measurement of .1 cm. Estimate the maximum possible error in computing the volume of the cube

$$V = x^3$$

$$x = 20 \pm .1 \quad x_1 = 20 \quad \Delta x = .1$$

$$\frac{dV}{dx} = 3x^2$$

$$V \pm dV = 8,000 \pm 120 \text{ cm}^3$$

$$dV = 3(20^2)(.1)$$

$$dV = 120$$