

$$324 - 576 + 270 = 18$$

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Activity 4.4: Contextual Situations. Applications of the Definite Integral

Name Elthon Gonzalez Ceniza ID A01510114 Date 12/March/2027

Using your knowledge on Calculus solve the following

1. A particle moves along a path with a velocity given by $v(t) = t^3 - 8t^2 + 15t$ in meters/second.

- a) Find the displacement of the particle on the first 6 seconds 18m
 b) Find the total distance traveled by the particle on the first six seconds 15.75 + 5.33 + 7.58 = 28.66

$$x(t) = \int_0^6 t^3 - 8t^2 + 15t = \frac{t^4}{4} - \frac{8t^3}{3} + \frac{15t^2}{2} = 0 \left[\frac{156.25}{4} - \frac{333.33}{3} + \frac{187.5}{2} \right] = 18m$$

2. An object moves on a linear path with a velocity given by $v(t) = \cos(2t)$ in meters/second.

- a) Find the displacement of the object from $t=0$ until $t=\pi$ seconds 0m
 b) Find the total distance traveled by the object from $t=0$ until $t=\pi$ seconds 2m

$$x(t) = \int_0^\pi \cos(2t) = -\frac{1}{2} \sin(2t) = 0$$

3. The acceleration of a particle, traveling along a linear path, is given by $a(t) = \sin(t)$ in meters/second², the particle starts from rest.

- a) Find the equation that gives the velocity of the particle $v(t) = -\cos(t) + C$
 b) Find the displacement of the particle on the first $3\pi/2$ seconds 1m
 c) Find the total distance traveled by the particle on the first $3\pi/2$ seconds 3m

$$-\cos(3\pi/2) = 0 \quad \int_0^{3\pi/2} -\sin(t) = \cos(t) = 1 - (-1) = 2$$

4. An object is moving along a path in such a way that the acceleration of the object is given by $a(t) = \frac{1}{\sqrt{t+1}}$ in meters/second².

- a) Find the equation that gives the velocity of the object, the initial velocity of the object was 2 $v(t) = 2(t+1)^{1/2} + 4$
 b) Find the displacement of the object from $t=0$ until $t=4$ seconds 2.42m
 c) Find the total distance traveled by the object from $t=0$ until $t=4$ seconds 2.9m

By: Teachers that Designed the Course
 Translated by: Arq. Mónica M. Paniagua

$$\int_0^4 \frac{1}{\sqrt{t+1}} = 2 \left[\frac{2}{3} (t+1)^{3/2} + 4t \right] = 2.60$$