

# GeoGebra<sup>4</sup>

## Quickstart

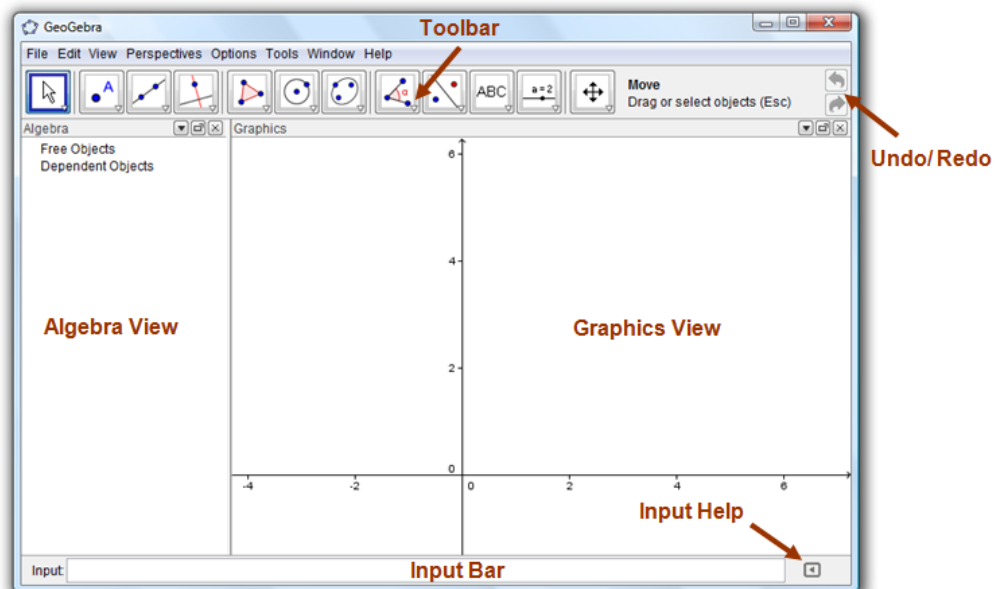
### What is GeoGebra?

- Dynamic Mathematics Software in one easy-to-use package
- For learning and teaching at all levels of education
- Joins interactive **geometry**, **algebra**, tables, graphing, calculus and statistics
- Open source software, freely available from [www.geogebra.org](http://www.geogebra.org)

### Quick Facts

- GeoGebra facilitates the creation of mathematical constructions and models by students that allow interactive explorations by dragging objects and changing parameters.
- GeoGebra is also an authoring tool that allows teachers to create interactive web-pages. Find interactive classroom materials and share your own work on [www.geogebraTube.org](http://www.geogebraTube.org).

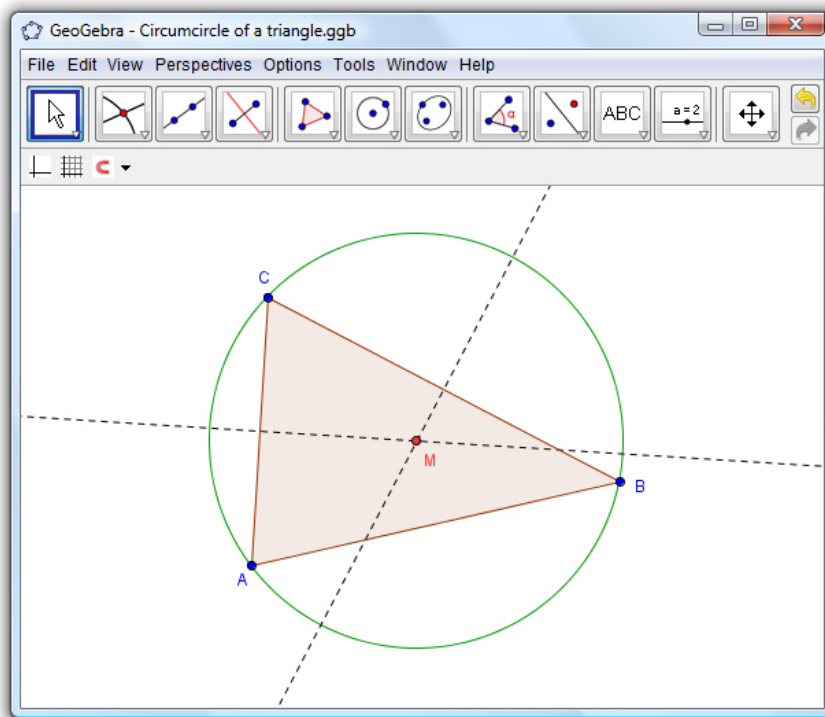
After starting GeoGebra, the following window appears:



By means of construction tools in the **toolbar** you can do constructions on the **graphics view** by mouse. At the same time the corresponding coordinates and equations are displayed in the **algebra view**. The **input bar** is used to enter coordinates, equations, commands and functions directly; these are displayed in the graphics view and in the algebra view immediately after pressing the Enter key. In GeoGebra, geometry and algebra work side by side.

## Example 1: Circumcircle of a Triangle

Task: Construct a triangle  $A, B, C$  and its circumcircle using GeoGebra.








### Construction Using the Mouse

#### Preparations

- Open the *Perspectives* menu and select *Geometry*.

#### Construction Steps

1		Choose the tool " <i>Polygon</i> " from the toolbar. Now click on the graphics view three times to create the vertices $A, B$ , and $C$ . Close the triangle by clicking on point $A$ again.
2		Next, choose the tool " <i>Perpendicular Bisector</i> " (click on the small arrow at the fourth icon from the left) and construct two line bisectors by clicking on two sides of the triangle.
3		Using the tool " <i>Intersect Two Objects</i> " you can click on the intersection of both line bisectors to get the center of your triangle's circumcircle. To name it " $M$ ", right-click on it (Mac OS: ctrl-click) and choose " <i>Rename</i> " from the appearing menu.
4		To finish your construction, choose the tool " <i>Circle with center through point</i> " and click first on the center, then on any vertex of the triangle.
5		Using the " <i>Move</i> " tool you can now use the mouse to drag the triangle vertices around - your construction will change dynamically with them.

## Some tips




Try the “Undo”/ “Redo” buttons on the right side of the toolbar.



To **hide an object**, right click on it (Mac OS: ctrl-click) and uncheck “Show Object”.



You can change the **appearance of objects** (color, type of line, ...) easily using the style bar: just click  at the top of the graphics view to show or hide it. For more options, please right-click (Mac OS: ctrl-click) on an object and choose “Object Properties” from the appearing context menu.



**Axes** and **grid** can be hidden or shown using the “View” menu just like the **algebra**, **graphics**, and **spreadsheet** view.



In order to **move your construction** in the graphics view, choose the tool “Move Graphics View” and simply use the mouse to drag it.

The **construction protocol** (see View menu) provides a table with all the steps of your construction. Using buttons you can step through the construction steps again. Furthermore, you can drag lines to change the construction order.

## Construction using the Input Bar

### Preparations

- We are now going to do the same construction as above using the input bar, so we will start from scratch by using *New* in the *File* menu.
- Open the *Perspectives* menu and select *Algebra & Graphics*.

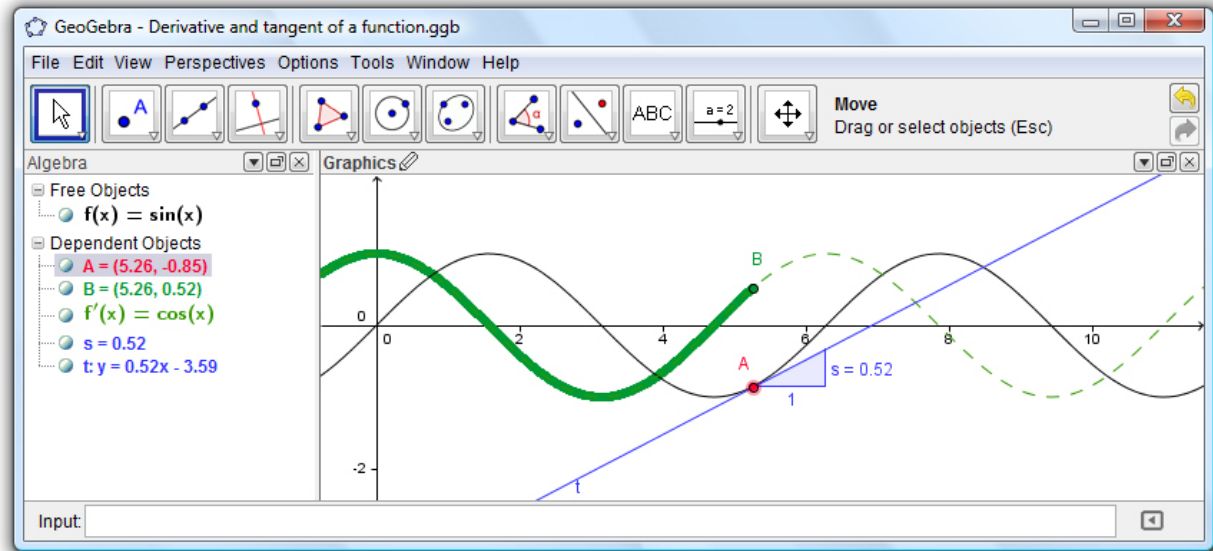
### Construction Steps

Type the following commands into the input bar at the bottom of the screen and press the Enter key after each line.

```
A = (2, 1)
B = (12, 5)
C = (8, 11)
Polygon[A, B, C]
s = PerpendicularBisector[a]
t = PerpendicularBisector[b]
M = Intersect[s, t]
Circle[M, A]
```

## Example 2: Derivative and Tangent of a Function

**Task:** Create the function  $f(x) = \sin(x)$ , its derivative and its tangent to a point on  $f$  including its slope triangle.








### First Way: Point on function

#### Preparations

- Open a new window using *New Window* from the *File* menu.

#### Construction Steps

1	$f(x) = \sin(x)$	Type the function $f(x) = \sin(x)$ into the input bar and press the Enter key.
2		Choose the tool “ <i>New Point</i> ” and click on the function graph of $f$ . This creates point $A$ attached to the function $f$ .
3		Now choose the tool “ <i>Tangents</i> ” and click on point $A$ and function $f$ . Change the tangent’s name to “ $t$ ” by using right-click (Mac OS: ctrl-click) and “ <i>Rename</i> ”.
4	$s = \text{Slope}[t]$	Type the command $s = \text{Slope}[t]$ .
5		Using the “ <i>Move</i> ” tool, drag point $A$ with your mouse and observe the movement of the tangent.
6	$B = (x(A), s)$	Type $B = (x(A), s)$ <u>Hint:</u> $x(A)$ gives the x-coordinate of point $A$ .
		Turn on the <i>trace</i> of point $B$ by right-clicking on $B$ (Mac OS: ctrl-click) and choosing “ <i>Trace On</i> ”.
7		Using the “ <i>Move</i> ” tool, drag point $A$ with the mouse – point $B$ will now leave a trace.
8	$\text{Derivative}[f(x)]$	Type the command $\text{Derivative}[f(x)]$

## Some Tips

Type a different function, e. g.  $f(x) = x^3 - 2x^2$ , into the input bar. Immediately, its derivative and tangent will be shown. Also try out the command `Integral[f(x)]`.



Choose the “Move” tool and drag the function’s graph with the mouse. Observe the changing equations of the function and its derivative.

**Automatic completion of commands:** after entering the first two letters of a command, it will be displayed automatically. If you want to adopt the suggestion, press the Enter key, otherwise just continue typing.



The **input help** is found on the right next to the input bar and gives you a list of all available commands in GeoGebra.

## Second Way: Point at $x = a$

### Preparations

- We are now going to do another version of the last construction. Therefore, choose *File – New* to get a fresh window.

### Construction Steps

Type the following commands into the input bar and press Enter after every line.

```
f(x) = sin(x)
a = 2
T = (a, f(a))
t = Tangent[a, f]
s = Slope[t]
B = (x(T), s)
Derivative[f]
```

## Some Tips

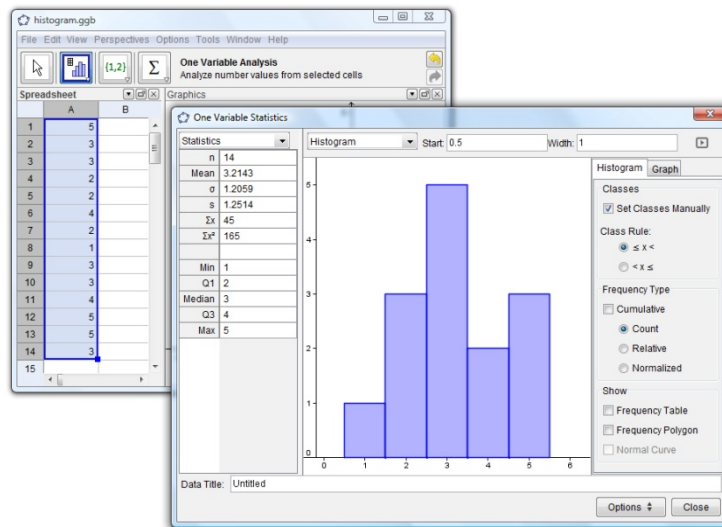


Choose the “Move” tool and click on the number  $a$ . You can change  $a$  by pressing the arrow keys. At the same time, point T and the tangent will move along the function  $f$ .

You can also change the number  $a$  by creating a **slider**: right-click (Mac OS: ctrl-click) on  $a$  in the algebra view and choose “Show Object”. Change the slider value by dragging the appearing point on the line with the mouse.

## Example 3: Analyzing Data

**Task:** Create a histogram and evaluate mean, median, min and max of a number of values.



### Preparations

- Open the *Perspective* menu and select *Spreadsheet & Graphics*

### Construction Steps

1		Enter some data into the cells of column A of the spreadsheet, e.g. fill A1 to A14 with values like 5, 3, 3, 2, 2, 4, 2, 1, 3, 3, 4, 5, 5, 3
2		Highlight the appropriate cells and select the tool “ <i>One Variable Analysis</i> ”. <u>Hint:</u> In this example: Highlight the cells A1 till A14 and click the tool “ <i>One Variable Analysis</i> ”.
3		Select the appropriate “ <i>Classes</i> ” at the top of the pop-up window. <u>Hint:</u> For the numbers in this example 5 <i>Classes</i> were used, because there are five different values.
4		Find the mean, the median, the maximum and the minimum of the data in the “ <i>Statistics</i> ” part on the left side of the pop-up window.
5		Click the arrow button at the top right and select “ <i>Set Classes Manually</i> ” in the right “ <i>Histogram</i> ” menu. <u>Hint:</u> Press “ <i>Enter</i> ” after specifying the “ <i>Start</i> ” value 0.5 and the “ <i>Width</i> ” 1 (values of this example).

### Some Tips

Change some values in column A and see how this influences the histogram and the statistical values like mean, median, maximum and minimum.

Change the diagram type from “*Histogram*” to “*Box Plot*” in the list box above the histogram.

## Further Information

You can find further information, materials and help on our web pages:

Software

<http://www.geogebra.org>

Manual & Tutorials

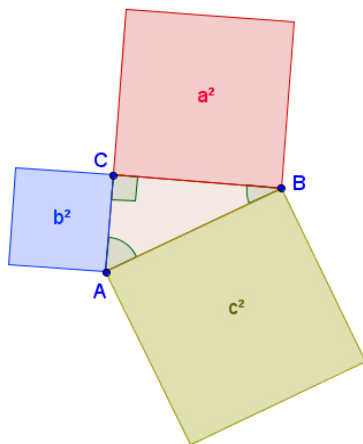
<http://wiki.geogebra.org>

Worksheets & Materials

<http://www.geogebraTube.org>

User Forum

<http://www.geogebra.org/forum>



$$\begin{array}{l}
 a = 10.36 \quad a^2 = 107.29 \quad a^2 + b^2 = \\
 b = 6.01 \quad b^2 = 36.15 \quad 107.29 + 36.15 = 143.44 \\
 c = 11.98 \quad c^2 = 143.44 \quad a^2 + b^2 = c^2
 \end{array}$$

